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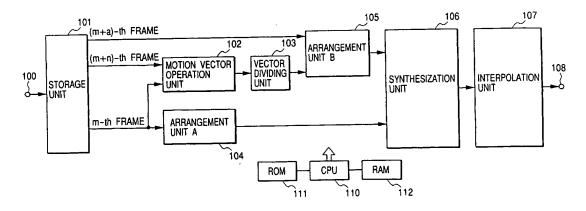
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(54) Image processing method and apparatus

(57) There is disclosed a method for obtaining one high-resolution image from a plurality of low-resolution images having predetermined resolutions, comprising steps of detecting relative positions among the plurality of low-resolution images with a resolution less than a pixel pitch in the predetermined resolutions, and forming a new image having a high resolution as compared with the predetermined resolutions using the plurality of images in accordance with information indicating the rela-

tive positions, so that the high-resolution image is obtained without any disorder. Moreover, there is disclosed a method for detecting motion vectors among a plurality of frames with a higher resolution, comprising steps of using orthogonal transform coefficients of images in the plurality of frames in motion images to detect the motion vectors among the plurality of frames with the resolution less than the pixel pitch in the predetermined resolutions

FIG. 4



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Description

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BACKGROUND OF THE INVENTION

Field of the Invention

[0001] The present invention relates to image processing method and apparatus, particularly to method and apparatus for forming a high-resolution image from a low-resolution image, motion vector detecting method and apparatus for use together with the image processing apparatus, method and apparatus for synthesizing a plurality of images, further to a recording medium readable by a computer which is used in these methods and apparatuses, and the like.

Related Background Art

[0002] Various methods have been heretofore proposed as methods for converting the resolution from inputted low-resolution information to high-resolution information.

[0003] In the conventional proposed resolution converting methods, a high resolution is realized by interpolating pixels to the low-resolution information, and the conversion processing method differs with the type of the object image (e.g., a multivalued image in which each pixel has gradation information, a binary image binarized by a pseudo intermediate gradation, a binary image binarized by a fixed threshold value, a character image, and the like).

[0004] As the pixel interpolating method in the conventional resolution converting method, a closest interpolating method of arranging the same pixel value closest to an interpolation point as shown in Fig. 1, a common primary interpolating method of determining the pixel value of an interpolation point E by the following operation in accordance with the distances of four points (four point pixel values are set to A, B, C, D) surrounding the interpolation point as shown in Fig. 2, and the like are generally used.

$$E = (1-i)(1-j)A+i(1-j)B+j(1-i)C+ijD$$
 (1)

(when the distance between pixels is set to 1, the interpolation point E has a distance i in a transverse direction and a distance j in a vertical direction from A (i≤1, j≤1)).

[0005] Moreover, as heretofore represented by a sampling theorem, means for converting a sampled discrete signal to a continuous signal comprises passing the signal through an ideal low pass filter which can be represented by SINC function, so that the continuous signal can be reproduced. Moreover, since the operation of SINC function requires much processing time, there is proposed another method which comprises approximating the interpolation function represented by the SINC function, and calculating an interpolated value only by a simple operation of sum of products. [0006] For example, in a known cubic convolution interpolating method, the approximating of the interpolation function can be realized. A method of calculating the interpolated value by the interpolating method will be described with reference to Fig. 3. In the pixel arrangement shown in Fig. 3, P denotes an interpolated point (interpolation point), and P11 to P44 denote pixel values of 16 pixels surrounding the point. Then, the interpolation point is interpolated using a cubic convolution function shown in the following equation. Additionally, in the following equation, x^y represents y power of x.

$$P = [f(y1)f(y2)f(y3)f(y4)] \begin{bmatrix} P11 & P12 & P13 & P14 \\ P21 & P22 & P23 & P24 \\ P31 & P32 & P33 & P34 \\ P41 & P42 & P43 & P44 \end{bmatrix} \begin{bmatrix} f(x1) \\ f(x2) \\ f(x4) \end{bmatrix}$$

... (2)

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$$f(t) = \sin(\pi t)/(\pi t)$$

$$= \begin{bmatrix} 1-2|t|^2+|t|^3 & (0 \le |t| < 1) \\ 4-8|t|+5|t|^2-|t|^3 & (1 \le |t| < 2) & \dots & (3) \\ 0 & (2 \le |t|) \end{bmatrix}$$

$$x1 = 1+(u-[u])$$
 $y1 = 1+(v-[v])$
 $x2 = (u-[u])$ $y2 = (v-[v])$... (4)
 $x3 = 1-(u-[u])$ $y3 = 1-(v-[v])$
 $x4 = 2-(u-[u])$ $y4 = 2-(v-[v])$

[0007] (In the equation, [] denotes Gauss' notation, and takes an integer portion.)

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[0008] However, as a result of resolution conversion by the above-described three types of interpolating methods, a blur by interpolation, and a block-shaped jaggy dependent on input low-resolution image occur, and high quality and resolution information cannot be prepared.

[0009] To prepare the high-resolution information from the low-resolution information in such background, there is also proposed an interpolating method including a technique of realizing the resolution conversion without generating the interpolation blur attributed to the interpolating processing or the jaggy, a technique of preparing an excellent edge while maintaining the continuity of pixel values, and the like.

[0010] However, the resolution conversion by the above-described conventional interpolating method has the following defect. Specifically, even if the high-resolution information is prepared, the enhancement of image quality is limited.

[0011] As apparent from the sampling theorem, since the information with the input resolution equaling or exceeding Nyquist limit does not exist in the input image, the preparation of information with Nyquist frequency or more frequency is all based on presumption. Therefore, it is easy to convert flat artificial images such as not-complicated CG image, illustration image, and animation image to jaggy-less images, but it is difficult to enhance the image quality of a natural image by presuming the information equaling or exceeding the Nyquist limit. Specifically, even if any method is used, the image quality of the image obtained by inputting low-resolution information and converting the resolution to a high resolution is evidently deteriorated as compared with the image inputted originally as the high-resolution information.

[0012] On the other hand, with the spread of digital video cameras in recent years, it becomes easy to input the picked-up motion image into a computer in the unit of continuous one frame. Therefore, one frame of motion image can also be outputted via a printer. However, as compared with the yearly increasing output resolution of the printer, the input resolution of a picking up system tends to increase, but it is still low in the present situation.

[0013] Therefore, as described above in the conventional example, instead of preparing one frame of high-resolution still image from one frame of low-resolution still image, it is considered that one frame of high-resolution still image is prepared from a plurality of continuous low-resolution still images taken from the motion image.

[0014] The technique of preparing the high-resolution still image from the low-resolution motion image is proposed in Japanese Patent Application Laid-Open No. 05-260264. The proposed method comprises comparing images continuous in point of time, detecting parameters of affine transformation and parallel movement based on the difference of the images, and synthesizing these images. Additionally, an example in which the synthesizing method is utilized for interpolation is also mentioned.

[0015] However, this proposal has the following problem:

[0016] Specifically, in the method of utilizing the synthesizing method for the interpolation, by comparing the continuous images enlarged by the interpolating method shown in Figs. 1 to 3, the parameters are calculated to determine an interpolation position, before performing the synthesis. However, for the enlarged image obtained by the interpolation in this manner, new high-resolution information is not prepared by the interpolating operation itself. Therefore, even when the synthesis processing is performed using the enlarged image in this manner, a really high-resolution image is not necessarily obtained.

[0017] Here, the interpolation indicates the interpolation between the pixels. In the interpolation by the synthesizing method, however, when the continuous images are compared, there is not information between the pixels for creating

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- \1176^ Gjn/!5ljt blcmpdl lejbhsbn lti px johlu flgvodypobnodpot yw ypologbldpn qv ufslbt lboljn bhf lqspdftt johlbqqbsbwt
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 uplGjh/!5/!Beejypobnoo-ljolu flfn cpejn fou-lbolfybn qufnlxjmhofleftdsjcfeljolxijdilu fljn bhflqjdlfe.vqlczlblejhjubnhojefp
 dbn fsb!jtlubotnjufeluplbldpn qv ufslboe!usbotgpsn feluplqspwjef!blsftpmujpoldpssftqpoejohluplu bulpgblqsjoufslcz
 bqqmidbypoltpgx bsfljolu fldpn qv ufsl
- \1177^ Gh/!5ltipxt!b!cmpdi!ejbhsbn!pgb!gvodujpo!pgb!dpnqvufstqsftfoufe!bt!bo!jnbhf!qspdfttjoh!bqqbsbwt!pguf

 Gtufncpejnfoulpguffqsftfoujowfoujpo/!!fsfjobgfsbo!pqfsbujpo!tfrvfodf!pguffdpnqvufsljt!fyqmbjofe!jo!sfgfsfodf

 p!Gh/!5/!.b!ujt!fncpejnfou!jujt!fyqmbjofe!bt!bo!fybnqmf!ubbo!jnbhf!qjdlfe!vq!cz!b!ejhjubmwjefp!dbnfsb!jt

 usbotnjufe!up!uff!dpnqvufsboe!uffo!dpowfsfe!joup!bo!jnbhf!pgsftpmwjpo!dpssftqpoejoh!up!ubupgb!qsjoufslcz!bo

 bqqmdbypo!tpgxbsf!tupsfe!jo!uff!dpnqvufsf

\\\ \tag{1179^\tag{115ef opuft! bolbsebohf n fouvojuB!\text{up!dpousprhii f !qiyf ribsebohf n foulpgui f !qidl fe.vq!\text{in bhft /!N psf.} pwf s!\text{bolbsebohf n fouvojuC!216!dpousprh!\ti f !qiyf ribsebohf n foulp!\text{couift!} of sqprhoufe!\text{up!\ti f !\text{in bhft k ju !\ti f !qiyf ribsebohf e cz!\ti f !\text{bsebohf n fouvojuB!215!jo!bddpsebodf! x ju !\ti f !\text{in pvouppdwfd.pst !ej\text{up} f !\text{vi f !\text{m} dups!ej\text{up} ej\text{up} ej\text{up} el\text{vi f !\text{up} dups!ej\text{up} el\text{up} el\text{vi f !\text{up} dups!ej\text{up} el\text{up} el\text{vi f !\text{up} dups!ej\text{up} el\text{up} el\text{vi f !\text{up} bhft! x ou f t if !\text{up} bhft! x ou f t if !\text{up} bhft! x ou f t if !\text{up} el\text{up} el\te

\117: ^ Ovn f sbrt221lef opuf t IDQV k i jdi kdpousprhlu f lpqf sbujpolpdf bdi kdpot ujuvujpolef t dsjcf e lbcpwf ijolblhf of sbrtjoln n boof sljolbddpsebodf lx ju lu f ldpousprhqsphsbn li f reljolSPN l222-lboelSBN l223ljt lvt f elbt lu f lpqf sbujpolbsf blpdu f DQV l221/

\1181^ B!qspdfttjoh!jolu f!n pypolwfdups!pqfsbypo!voju213!xjmfofyucf!eftdsjcfe!jolefubjrfn

\1182^ Wospvt in fui pet kgosklohodvrhoujoh kui fin pujpo kwf dupsti bwf kcffo kqspqptfe-kcvulb in fui pelvtjoh kt p.dbmfnek fin qmbuf n budi joh kx jmmlof left dsjcfeli fsfjob gfs/

\1183^ Bt!tipxoljo!Gh/!6-lb!tin qmut!psblcmod!!ibwjoh!O2 ×!O2!qjyfm!jt!n pwfe!po!b!tfbsdi!sbohf!)N2!.!O2!, !2*
_3!jo!b!mshfsljoqvuljn bhf!x ju !N2 ×!N2!qjyfmh-!boe!u f!mglvqqfslqptjujpo!pgb!tin qmut!jn bhf!jt!pcubjofe!jo!xijdi
u f!sftjevbmsfqsftfotfe!cz!u f!gpmpxjoh!frvbujpo!)6*!jt!n jojn vn /!.b!u jt!dbtf-!n budijoh!jt!sfhbsefe!bt!i bwjoh!cffo
bdijfwfe/

S)b-c* > TT}Jb-c*)n 2-o2*.U)n 2-o2*}

)6*

\1184^),b!ú f !f r vbýpo-lú f !rhgiT!jt !jo!ú f !sbohf !pgn rh>!1!ψ!O2.2-!boe!ú f !sjhi uT!jt !orh>!1!ψ!O2.2/*

41

66

\1185^ Beejypobnon-jolu f frvbupon6*-nb-lc*joejdbuft lu f lingl/vqqf slaptjypologu f lu n qnbuf jn bhf jolu f joqvujn bhf-lboe!Un 2-lo2*ljoejdbuft lu f labsybnim bhf logu f lioqvujn bhf-lboe!Un 2-lo2*ljt lu f lu n qnbuf jn bhf/

1186^ _blu jt ldbtf-lx i folu f !n budi joh!efwjbuft-lu f !st tjevbrijt !sbqjenzlijodsf bt felevsjoh!t fsjbrlbeejujpo!pgu f !qjyfnt/
Lb!t pnwf !u f |qspcrfnn-lb!sft jevbrht frvfoujbrhuft ujoh!n fu pe!dpn qstft !kvehjoh!u bulu f !n budi joh!jt !jotvojDijfoux i fo
u f !sft jevbrht ydffet !b!dfsubjo!u sft i pne!wbrwnf!evsjoh!u f!beejujpo!t i pxo!jo!u f !frvbujpo!)6*!up!t upq!u f!beejujpo-!boe
t i jajoh!up!u f !ofyulpqfsbujpo!pg)b-!c*/

\1187^ Tqf djÖdbnask i foljdjt lbt t vn felu bdux pluzqf t lpgjn bhf t lbsf ldpoljovpvt ljn bhf t !polbojn bujpo-!cz!vt joh!u f bopwf.eft dsjcfeln f u pe-!u f lhf pn f usidlef wjbujpo!cf ux f folcpu ljn bhf t ldbo!f bt jnz!cf !r vboujubujwf nz!ef uf sn jof e/

1188^ Bt!uif!n pujpo!widups!pqfsbujpo!n fuipe!b!ijhifsqsidjtjpo!n fuipe!ibt!bmp!cffo!qspqptfe-!cvulup!gbdjmjobufuif!eftdsquipo-!uif!bcpwf.eftdsjcfe!n fuipe!cz!uif!ufn qmbuf!n budijoh!jt!vtfe!jo!uif!fn cpejn fou

\1189^ Beejypob noo-logsluif!n pypo!wfdpslcz!uif!ufn qnbuf!n budijoh-!uif!n budijoh!jo!xijdi!uif!sftjevbrhjt!n jojn vn jt!efufdufe-!boe!uif!sftpmujpo!pduif!wfdpsljt!b!qjyfnhvojubt!eftdsjcfe!bcpwf/!TqfdjÖdbnoo-log!sftpmujpo!Ofssuibo!uifejtwbodf!cfuxffolqjyfnhljt!qspwjefe/!Ujt!wfsz!fggfdywf!up!vtf!uif!ufn qnbuf!n budijoh!bt!n pypo!dpn qfotbypo!evsjohdpejoh-!cvUgpsluif!bqqnjodypo!up!uif!joufsqpnbujpo-!uibuljt-!uif!joufsqpnbujoh!ufdiojrvf!pgÖnjooh!uif!jogpsn bypo!cfuxffouif!qjyfnh-!b!Oofslsftpmujpo!t!ofdfttbsz/

\118: ^ Ui f sf gosf-ljo!ui f !f n cpejn f ou!jot uf be!pgdbrotvrhujoh!ui f !n pujpo!wf dups!pgux p!uzqf t !pgjn bhf t !bqbsulgspn !f bdi !pui f sjo!t bn qrjoh!ujn f !jt !dbrotvrhuf e/

\\ \tag{1191^ TqfdjOtbmo-lgslux pluzqft!pgjn bhft!usbotn jufe!upluif!n pujpo.\wfdupslpqfsbujpo!vojul213!gspn!uif!t upsbhf!voju\\ \tag{212-!pof!jn bhf!jt!b!dfsubjo!jn bhf!}) if sfjobgfslsfgfsefe!up!bt!uif!n .ui!gsbnf*!jn nfejbufzo!bgfsluif!vtfsljttvft!uif qjdl vq!dpn n boe-!boe!uif!puifsljn bhf!jt!o.ui!gsbnf!bgfsluif!n .ui!gsbnf!) if sfjobgfslsfgfsefe!p!bt!uif!)n, o*.ui!gsbnf-o?2*/!Bo!fybn qmf!pgo!>!4!xjmmopx!cf!eftdsjcfe/!.b!uif!n pujpo!wfdupslpqfsbujpo!vojul213-!uif!hfofsbujpo!pgwfdupsn pwfnfouljt!efufdfe!cfuxffo!n .ui!gsbnf!jn bhf!boe!)n, 4*.ui!gsbnffjn bhf/!Pgdpvstf-!uif!sftpmujpo!pguif!n pujpo wfdupsldboom/moufe!buuijt!unf!jt!b!qjyfmvoju!boe!jt!frvbmup!b!qjyfmqjudi/

\1192^ Ui f !qspdf t t joh!jo!ui f !wf dupslejwjejoh!vojul214!x jmhof yulcf !ef t dsjcf e!jo!ef ubjrh

\1193^ Uif!wfdupslejwjejoh!vojul214!jt!dpot ujuvufe!pgb!ejwjefstxijdi!qfscpsnt!ejwjtjpo!xjui!b!wbrwf!pgo!up!dpowfsuluif wfdupslon pvouh pwfelon pohluif lotgston ft lup!uif!wfdupslon pvouhqfstgston flobtfelpo!uif!n pujpo!wfdupslon pvouhdbrdvrhoufe

jo!u f !n pypo!wf dups!pqf sbypo!voju213/

\1194^ Bt !eft dsjcfe!bcpwf-!pof!dibsbduf sjt yjd!pg'uif!fin cpejn foulrjit!jo!uibluif!sft pravjpo!pg'uif!n pypo!wfdupsljt
tfulp!cf!Oofsluibo!uif!cfuxffo.qjyfntejtubodf!)qjudi*!up!qfsgpsn!uif!joufsqpravjpo/!ub!uif!fn cpejn fou!juljt!bttvn fe
uibluif!n pypo!wfdupsldpn qm'ufmzljoofbsmz!n pwft!jo!qpjoulpg'yinf/IX ifo!uif!n pypo!wfdupslrjnofbsmz!n pwft!jo!uijt!n boofs
czldbradvrbujoh!uif!n pypo!wfdupslbulyinf!joufswbrhlpgbkqrasbrjnoz!pggdonft!boekdpowfsujoh!uif!wfdupslbn pvoulup!uif!bn pvou
qfslgbnf-!uif!wfdupslOofsluibo!uif!cfuxffo.qjyfntejudi!dbo!cf!dbradvrbuufe!bn poh!uif!dpoyjovpvt!gsbnft/

\1195^ Beejypobnoo-lt jodf luif !f n cpejn foujt !f tubcrjn i fe!cbt fe!po!uif!bcpwf.eft dsjcfe!bt tvn qupo-!uif!gonpox joh trjm i usft usjdypo!bqqrjn t/!Tqf djÖdbnoo-!x i fo!uif!bn pvoulpguif!n pujpo!wf dups!bn poh!uif!o!gsbn ft!jt!f ydft tjwf no!noshf bt!dpn qbsfe!x jui!uif!wbnqf!pgo-!uif!qsfdjtjpo!pguif!wf dups!bn pvoulqfs!gsbn f!jt!efufsjpsbufe!jo!t pn f!dbtft/

\1196^ X i folu f!pckfdujn bhf!jt!opub!sbqjerz!n pwjoh!jn bhf!t vdi!bt!t qpsut df of -!cvujt!b!sf haywfrz!fntt!n pwjoh
jn bhf!pgdpn n f n psbywf!qjdl joh.vq-!t df of sz-!qrbou!t ymhjgf-!pslui f!mhff-!ui f!bct prnuf!n pwf n foulbn pvouljt!t n bmjo
n boz!crpdl t!pgui f!jn bhf/!Ui fo-!jo!ui f!n pujpo!wf dupslef uf dyoh!n fui pe!cz!ui f!uf n qrbuf!n budi joh!t i px o!jo!Qjh/!6-!ui f
n pujpo!bn pvoulobuvsbrzz!ejggfst!x jui!ui f!crpdl!voju!Ui fsfgpsf-!jujt!dpotjefsfe!ui bului f!crpdl!i bwjoh!b!rbshfsln pwf n fou
bn pvoului bo!b!qsfef uf sn jof e!wbrwf!jt!dpot yjuvuf e!opulup!cf!ejwjefe/

QiyfntBssbohfn foulPvunjof

\1197^ Ui f!bssbohf n f ouvojuB!215!bssbohf t!n .ui !gsbn f!qjyf rh-!boe!ui f!bssbohf n f ouvojuC!216!bssbohf t!jouf sqp. rhujpo!qjyf rh!up!ui f!n .ui !gsbn f!jn bhf!jo!bddpsebodf!x jui !ui f!wf dups!ejwjejoh!bn pvou!Tqf djÖdbrab!ui f!gsbn f!joqvuf e!up ui f!bssbohf n f ouvojuC!216!jt!n , b.ui !gsbn f!jb>!2!up!)o.2**-l)o.2*!gsbn f!qjyf rh!bsf!t f sjbraaljoqvuf e-!boe!ui f!qjyf rhwbraf t pdui f!jouf sqprhaujpo!qjyf rh!bsf!bssbohf e!jo!bddpsebodf!x jui !ui f!ejwjejoh!bn pvouf

\1198^ __blu jt ldbtf-lu f lejwjejohlon pvoulusbot n juf elgepn lu f Mrdupslejwjejohlvojul214ljt l20o lpgu f ln pujpolwf dupsk i jdi jt ln vnajqnjfi elczlbljolu f !bssbohf n f ouvojulCl216/!Tqf djÖdbnazelu f !n pujpolwf dups ×!)b0o*!joejdbuf t !u f !bssbohf n f ou qpt jujpolx i f olu f !)n , b*.u !gsbn f !jt !joqvuf e/

\1199^ If st-ljolu f!fybn qm!pgo!>!4-!tjodf!u f!bssbohfn fouvojuC!216!st dfjwft!204!bt!u f!ejwjejoh!bn pvoupgu fn pujpo!wfdups!204!pgu f!n pujpo!wfdups!jt!bssbohfe!jo!u f!)n, 2*.u lgbn f-!boe!304!pgu f!n pujpo!wfdups!jt!bssbohfe!jou f!)n, 3*.u lgbn f/

\119: ^ Ght //TBlup!7E!bsf !ejbhsbn t !t i px joh!f ybn qrfit !pgbdwbrijn bhf !n pujpo/!Jb!ui f !f ybn qrfi!b!qidl f e.vq!pclf du/
)psbldbn f sb*lhsbevbrazin pwf t ijolbolpcrja vf !ejsf dujpo/!Ght //TBlup!7E!t i px !n .ui !up!)n , 4*.ui !gsbn f ijn bhf t !sf t qf dujwf rz/
\11: 1^ Ght /!8B!up!8D!t i px !ui f !t ubuf t !pgbi f !n pujpo!wf dupsljo!ui f !f ybn qrfi!t i px o!jo!Ght /!7B!up!7E/!Gh/!8B!t i px t
ui f !n .ui !gsbn f !jn bhf -!boe!Gh/!8C!t i px t !ui f !)n , 4*.ui !gsbn f !jn bhf /!! f sf -!ui f !jn bhf t !t i px o!jo!Ght /!8B-!8C!bsf !vt f e
bt !ux p!uzqf t !pgjin bhf t !gps!dbrdvrbujoh!ui f !n pujpo!wf dups!Jb!Ght /!8B!up!8D-!ui f !crpdl t !t vsspvoejoh!ui f !pc!f dulbsf !vt f e
bt !ui f !crpdl t !gps!dbrdvrbujoh!ui f !n pujpo!wf dups!boe!dpssf t qpoe!up!O2 ×!O2!crpdl t !t i px o!jo!Gh/!6/!Beejujpobraze!up
dpdjrjabuf !ui f !ef t dsjqujpo-!juljt !bt t vn f e!ui bului f !n pujpo!wf dups!jt !dpn n po!up!braterpdl t /!Ui f !n pujpo!wf dups!pcibjof e!gspn
Ght /!8B-!8C!it !t i px o!jo!Gh/!8D/

\11: 2^ Ght/!9B!up!9D!tipx!uif!tubuft!pgejwjtjpolpguif!n pujpo.Widupstipxo!jo!Gh/!8D/!Gh/!9B!tipxt!uif!tobuft!pgejwjtjpolpguif!n pujpo.Widupstipxo!jo!Gh/!9B!tipxt!uif!ejwjejoh!pguif WidupstpgGh/!9B!up!204-lboe!Gh/!9D!tipxt!uif!ejwjejoh!pguif!widupstpgGh/!9B!up!304/!TqfdjÖtlomae!tjodf!uif!widupston pvoultipxo!jo!Gh/!9B!n pwft!gpsluisff!gstonft-luif!widupstonft/

\11: 3^ Ght/!: B!\p!: E!t i px !\u00ed f!t \u00fc\u00ed f!t \u00ed f!t \u00ed

\11: 4^ Ui f !qjyf rhbssbohf n f ouljo!û f !f n cpejn f oulx jmhcf !ef t dsjcf e!i f sf jobgf sljo!n psf !ef ubjrh

\11:5^ Ght/!21B!up!21D!b of lejbh obn tit i px joh luifit ubuf tip gwf dup slejwjt jpo ljolef ub jmboeljouf stif dypolopjout lpgWr sujdbm boeli psj{poub miusbjhi uhjooft ljoejdb uf lippt juppot/!Bo!b sepx!dpoofdujoh!djsdm!n bolit ljo!Gh/!21B!joejdb uf til if ln puppowf dup sldb molvmbuf e bon poh luifijn b h ft lpguif ln .ui lgon fiboel)n, o*.ui lgon f/!Uif lqsftvn feldb tf lpgo⊳!4 x jmbof left dsjcfe if sfjobgfs/

\11: 6^ Uif!n pýpolwfdysti px oljo!Gjh/!21B!n pwft!vplúf!rhglcz!uisff!qjyfrhlboe!vqx bse!cz!ux p!qjyfrh/!TqfdjÖdbmauif!wfdysln pwfn fodgoslúisff!gsbn ft!jt!ti px o!cz!uif!bsspx/!Bo!bsspx!dpoofdyoh!djsdrh!boe!usjbohrh!n bslt!jo!Gjh/!21Cti px t!uif!bn pvodpguif!wfdysln pwfe!cz!204/!TqfdjÖdbmau!juljt!bttvn fe!uibduif!qjyfrhpguif!djsdrh!n bsl!n pwft!vp!uifusjbohrh!n bsl!jo!uif!)n, 2*.uilgbn f/!Tjn jrbssau!bo!bsspx!dpoofdyoh!djsdrh!boe!dsptt!n bslt!jo!Gjh/!21D!ti px t!uif!bn pvoupguif!wfdyslpgGjh/!21B!n pwfe!cz!304/!TqfdjÖdbmau!juljt!bttvn fe!uibduif!qjyfrhpguif!djsdrh!n bsl!n pwft!vp!uifldspttn bsl!jo!uif!)n, 3*.uilgbn f/

\11: 7^ G|h/!22!tipxt!blt.ubuf!jobxijdi!uisff!gebnf!jogsnbijpo!pdn.uilgebnf-!)n, 2*.uilgebnf-!boe!)n, 3*.uilgebnf!bsf

bsbohfelboeltzou ftj{felcbtfelpolu flejwjejohlwfdupslbn pvoutlti pxoljol@jht/l21Blupl21D/lTqfdj@dbmoelu fln.u gbn fljogsn bujpol)djsdrfiln bsit *ljtlbsbohfelx ju pvubozln pwfn foubn pvoulu fl)n, 2*.u lgbn fljogsn bujpol)usjbohrin n bsit *ljtlbsbohfeljolu flqptjupolx i fsflu flwfdupsln pwftlczl204-lboelu fl)n, 3*.u lgbn fljogsn bujpol)dspttln bsit* jtlbsbohfeljolu flqptjupolx i fsflu flwfdupsln pwftlczl304/lCzldpouspnjohlu flbsbohfn fouljolu jtln boofslu fljou sqp. rbujpolbn pohlu flqjfrhldbolcflf yfdvu elbt ti pxoljol@jh/l22/

\11: 8^ __bhi f if ybn qrhit i px oljol@h/l22hi sf f. ijn f t ljouf saprhujpoljt isf brjiff eljolb. Mr sijdbrhejsf dijpo-boehi f ljouf saprhujoh pqf sbijpoljolb!i psj{polbrhejsf dijpo-lpsibophi f slwf sijdbrhejsf dijpoljt! f yf dvuf elcz! ii f !jouf saprhujpolvoju218/!.b! ii jt !dbt f - ii f !dpowf oijpobrhn f ii pet !t i px o!jol@ht /!2!up!4-!boe! ii f !jhif !bsf !sf hbsef e!bt !ii f !jouf saprhujoh!n f ii pe/

\11: 9^ Beejypobnoo-ljolu f ljod saprhayohln f u pelbddpsejohluplu f lf n cpejn f oulu f lajyf rhjogosn bypoljt lopulof df t t bsjrobsbohf eljolblef t jsf eljod saprhaypolapt jypolbn pohlu f lajyf rhvl.blu jt ldbt f-lx i f olu f ljod saprhayohlpaf sbypoljt lbaqrifie vt johlu f lajyf rhlf yubddf elboe lbsbohf elgopn lu f lpu f slgon f t lboe lu f lajyf rhlfgu f last t f olgon f -left jsf eljod saprhaypo apt jypoljogosn bypoljt ldbrodvrhufe/lX i f olblamsbrjoz lpgt ymin bhf t lbsf lt zou f t j{f e-lbt ldpn qbsf elx ju lpof lgon f lpgt ymin in bhf -lu f lajyf rhsf g saf elupljolu f ljod saprhayohlpaf sbypoljt ldmpt f sluplu f ljod saprhaypolapt jypo-lt plu bubli jhi f saf djt jpo jn bhf ldbolcf lasf qbsf e/

\11::^ Beejypob moz•lú f ldb tf lx i f sf lú f li jhi lsf tpm úpoljt lsf b mýf elcz ljouf sqpmb úpoh lú f lqjyf mhli b t lcf f o lef t dsjcf eljo ú f lf n cpejn f o u lcv djuh pf t lx jú pv ut b z joh lú b dú f lqsf t f o djowf o ýpoldbo lt jn jmb soz lcf lb qqmi elf wf o lx i f o lf o mb sh f n f o u n b hoj Čab úpoldi b o h f ljt lsf b mýf f e/

\1211^ Bt !eft dscfe!bcpwf-!bddpsejoh!up!uif!fn cpejn fou!cz!f yusbdyoh!uif!n pujpo!wf dupst!gpslb!qnwsbrjwz!pggsbn ft-boe!ejwjejoh!uif!wf dupst!cz!uif!ovn cfslpggsbn ft-!uif!sft pmujpo!pguif!n pujpo!wf dupstbn pvoulpguif!dpoujovpvt!gsbn ft dbo!cf!tfdup!cf!Öpfsluibo!pof!qjyfnvoju!Uifsfgpsf-!cz!tzouiftj(joh!uif!qnwsbrjwz!pggsbn ft!xjui!uif!sft pmujpo!Opfsuibo!pof!qjyfnvoju!Uifsfgpsf-!cz!tzouiftj(joh!uif!qnwsbrjwz!pggsbn ft!xjui!uif!sft pmujpo!Opfsuibo!pof!qjyfnvoif!ijhi.sft pmujpo!jn bhf!dbo!cf!hfofsbufe!n psf!fybdumzf

\1212^ Npsf pwf s!bt !dpn qbsf elx ju !x i f o!u f !n pujpo!wf dupst !pgu f !dpoujovpvt !gsbn f !bsf !dbrdvrbuf e-!u f !gsf r vf odz pgpqf sbujpot !pgu f !n pujpo!wf dupst !jt !sf evdf e-!t p!u bub!i jhi .t qf f e!qspdf t t joh!dbo!cf !sf brjkf e/

\1213^ Ui f sf gpsf-!t jodf !pof !gsbn f !pgi jhi .sf t pmujpo!t ymijn bhf !jogpsn bypo!dbo!f bt jmz!cf !qsf qbsf e-!gpsf ybn qrf-gpn !ui f !mpx .sf t pmujpo!t ymijn bhf !jogpsn bypo!qi puphsbqi f e!cz!ui f !wjef p!dbn f sb-!boe!pvuqvuuf e!wjb!ui f !qsjouf s!boe ui f !mjhf-!ui f !pvuqvulpgi jhi .r vbmjmz!jn bhf t!dbo!cf !sf bmjkf e!jo!ui f !jn bhf !qspdf tt joh!t zt uf n !up!qf sgpsn !dpn n vojdbypo cf ux f f o!ui f !bqqbsbuvt f t !ejggf sf ouljo!joqvu[pvuqvulsf t pmujpo/

\1214^ B!tfdpoelfn cpejn foupdu f!qsftfoujowfoupo!x jmtcf!eftdsjcfe!ifsfjobgfs

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31

66

\1215^ Gh/!23!jt !blcmdl !ejbhsbn !t i px joh!u f !grodypobhdpot ywypo!pgu f !dpn qvu sbt !u f !jn bhf !qspdf t t joh!bq.

qbsbwt !pgu f !t f dpoe!f n cpejn f ou!u f !t bn f !dpot ywypo!bt !u bdpgGh/!5!jo!u f !Öst uf n cpejn f ou!t !ef opu e!cz!u f
t bn f !sf gf sf odf !ovn f sbrh-!boe!u f !ef t dsjqypo!u f sf pgjt !pn juf e/

\1216^ Uijt!tfdpoe!fn cpejn fouljt!di bsbdufs{fe!jo!uibuxifo!pof!gsbnf!pgtymmjn bhf!jt!qsfqbsfe-!uxp!uzqft!pg jn bhft!bt!uif!dbmdvmbujpo!pckfdupgduf!n pujpo!wfdups!bsf!tvddfttjwfmz!txjudife-!boe!gvsuifs!tzouiftj{fe/

\1217^ _b!Gh/!23-!b!dpvouf sl: 11!dpvout !u f !gsf r vf odz!pgbssbohf n f oulcbt f e!polf bdi !ejwjef e!wf dupsljo!u f !bssbohf . n f oulvojuC!216/

\1218^ Bolf ybn qmljolx i jdi lui f !n pujpolwf dupstcf ux f f olui f !n .ui !gsbn f !boe!ui f !)n , o*.ui !gsbn f !jt !dbrodv mbuf e!jo!ui f t bn f !n boof sibt !ui f !Öst ulf n cpejn f ou !boe!)o.2*!gsbn f t !gspn !ui f !)n , 2*.ui !gsbn f !up!ui f !)n , o.2*.ui !gsbn f !bsf !bsfbohf e cbt f e!po!ui f !ejwjef e!wf dupstx jmlopx !cf !eft dsjcf e/

\\121:^ Tvctfrvfouzo-luif !qjyfrthossbohfnfoulcbtfe!po!uif!npujpo.wfdups!jt!qfsgpsnfe!jo!uif!bssbohfnfoulvojuB!215
boe!uif!bssbohfnfoulvojuC!216-!boe!tzouiftj{fe!jo!uif!tzouiftj{joh!voju217/lo!uijt!dbtf-!jo!uif!tzouiftj{joh!voju
217-lo!tzouiftj{fe!jnbhf!jt!dpnqrfuifelcbtfe!po!uif!qsfwjpvt!n.uilgbnf!up!uif!)n, o.2*.uilgbnf/!Uifsfgpsf-luiflqjyfm
bssbohfnfoulcbtfe!po!uif!)n, o*.uilgbnf!up!)n, 3o.2*.uilgbnf!jt!gvsuifstzouiftj{fe!po!uif!tzouiftj{fe!jnbhf/}
\\1221^ Bt!eftdsjcfe!bcpwf-!jo!uif!tfdpoe!fncpejnfou!uif!jnbhft!bewbodfe!cz!o!gsbnft!bsfltfsjbroo!dpnqbsfe!up
pcubjo!uif!npujpo!bnpvou!boe!uif!qjyfrth!bsf!tfsjbroo!bssbohfe!cbtfe!po!uif!ejwjefe!wfdups!pcubjofe!cz!ejwjejoh!uif

pcubjo!uif!n pujpo!bn pvou!boe!uif!qjyfmtlbsf!tfsjbmoo!bssbohfe!cbtfe!po!uif!ejwjefe!wfdupslpcubjofe!cz!ejwjejoh!uif n pujpo!bn pvoucz!o/!TqfdjÖdbmoo!bttipxoljo!Qjh/123-bttvn joh!uibucijoejdbuftboojoufhfskuif!n pujpo!wfdupsijtbocubjofe cz!)n, o×c*.ui!gsbnf!boe!)n, o×)c, 2**.ui!gsbnf-!boe!)n, o×c, b*.ui!gsbnf!jt!bssbohfe!gpslfwfsz!)o.2*!gsbnft!cbtfe po!uif!ejwjefe!wfdups!Tvctfrvfouno-!uijt!qspdfttjohljt!sfqfbufe!up!b!qsfefufsnjofe!vqqfsljnmjulwbmsf!cz!jodsfnfoujoh c!fbdi!cz!pof-!blijhifslrvbnjooz!boe!sftpmujpo!jnbhf!dbo!cf!pcubjofe/

1222^ Bit left dscfelbcpwf-!bddpsejoh!up!uif!tfdpoe!fncpejnfou!jo!beejujpo!up!uif!fggfdulpcubjofe!gspn!uif!Östu
fncpejnfou!uif!ovncfslpggbnft!gos!vtf!jo!qsfqbsjoh!pof!tujmljnbhfljt!jodsfbtfe!cz!tfujoh!uif!vqqfslmjnjuwbmf!pg
c!up!cf!mbshf-!uif!jnbhf!rvbmjnz!bgfsluif!joufsqpmbujpo!jt!gvsuifslfoibodfe/

\1223^ Beejypobraz-ljolu f !t f dpoe!f n cpejn f ou!u f sf !dbo!cf !qspwjef e!u f !jn bhf !qspdf t t joh!bqqbsbuvt !jo!x i jdi !u f sf t pmujpo!dpowf st jpo!cz!cf t ujn bhf !r vbrjaz!dbo!cf !sf brjiff e!cz!t f ujoh!u f !wbmf t !pgo-!c-!gpsff ybn qrfn-!up!f yqf sin f oubraz

pcubjof e!pquin vn !wbmf t/

\1224^ Ovsi f sn psf-ljuli bt !cf f olef t dsjcf eljo!u f !t f dpoe!f n cpejn f odu bdu f !dpvouf sl: 11!dpvout !u f !bssbohf n f ou gf r vf odz!jo!u f !bssbohf n f odvojuC!216-!cvdu f !ovn f sjd!wbmf !up!cf !dpvouf eljt !opdrjm juf e!up!u f !bssbohf n f odgf r vf odz-!boe!dbo!cf !boz!wbmf !bt !mpoh!bt !judbo!ef Obf !u f !t ubslujn joh!pgu f !of yun pujpo!wf dups!pqf sbujpo/

\1225^ Blu jself n cpejn f oupgu f last t f oujowf oupolx jmicf left dsjcf eli f sf jobgf s

\\1226^ Gh/!24!jt !b!crpdl !ejbhsbn !t i px joh!u f !gvodýpobridpot ýwýpo!pgu f !dpn qvu slbt !u f !jn bhf !qspdf t t joh!bq.
qbsbwt !pgu f !u jself n cpejn f ou!u f !t bn f !dpot ýwýpo!bt !u bupgGh/!5!jolu f !Öxt uf n cpejn f ou!t !ef opu e!cz!u f !t bn f
sf sf odf !ovn f sbrh-!boe!u f !ef t dsjqýpo!u f sf pgjt !pn juf e/

\1229^ TqfdjÖtbroo-!u f!gsbn f!up!cf!dpn qbsfe!x ju !u f!n.u !gsbn f!jo!u f!n pujpo!wfdups!pqfsbujpo!voju2112!jt!u f)n, o.d*.u !gsbn f!)d!>!1!up!o.3*!bddpsejoh!up!u f!tjuvbujpo/!X i jrfi!jodsf btjoh!u f!wbroof!pgd!cz!pof-!ux p!gsbn ft!bsfdpn qbsfe/!Fwfoljo!d!>!o.3-!x i fo!u f!n pujpo!wfdups!jt!tymodsfsbu bo!u f!qsfefu sn jofe!u sfti pre!wbroof-!tzou ftjt!jtopuqfspsn fe-!boe!u f!n.u !gsbn f!jn bhf!jt!pvuqvufe!bt!jujt/

\122: ^ __b!u f !bssbohf n f ouvojuC!216-!u f !)n , b*.u !gbn f !)b!>!2!up!)o.d.2**!jt !joqvuf e!gpsl)o.d.2*!gbn f t -!boe!u f qiyf rhybraf t !bsf !bssbohf e!jo!bddpsebodf !x ju !u f !wf dupslejwjef e!bn pvoulejwjef e!cz!)o.d*/

\1231^ Bt left dsjcfelbcpwf-lbddpsejohlupluif luijselfn cpejn fouljolbeejujpolupluif lfggfdulpcubjofelgspn luif lÖstulfn.

cpejn foulcztdbrotvnoujohluif n pujpolwfdupsporzact uxffoluiflgsbn fti bwjohlbolbqqspqsjbufln pwfn foulbn pvouluplqfsgpsn
bolbqqspqsjbufljoufsqpmbujpolqspdfttjoh-luifljn bhflrvbrjoozlogs stuifljoufsqpmbujpoljtlgvsuifstoi bodfe/

\1232^ Beejypobroz-ljolu f lÖst uluplu jælf n cpejn f out -lu f laspafftt johlpgdbrotvrbujohlu f ln pypolwf aluplu jælf n cpejn f out -lu f laspafftt johlpgdbrotvrbujohlu f ln pypolwf aluplus laspaf ljolapjoupgyn f li bt lcf f oleft dsjcf e-lcvulu f ln pypolwf aluplabolbrhuplcf labrotvrbuf e vujnkjjohlu f lash f t lcf gosf lu f ln .ui lash f /

\1233^ Npsf pwf sljolu f!Öxt duplu jself n cpejn f out-lu f!u n qrbuf!n budi joh!i bt!cf f olf yqrbjof elbt!u f!f ybn qrfn!pgu f n pupo!wf dupsdbrdvrbujoh!n f u pe-!cvdpu f sin f u pet!n bz!cf!vtfe/!Qpsf ybn qrfn-!x i f o!u f!n pwf n f odcf ux f f o!u f gbn f t!jt!pu f siu bo!u f!qbsbrdirtn pwf n f odlu f sf !jt!dpot jef sf e!b!n f u pe!x i jdi!dpn qst f t!dbrdvrbujoh!u f!n pwf n f od pdb!spubujpo!t zt uf n !bt!bo!bgDof !usbot gpsn bujpo!dpf gDdjf odlejwjejoh!u f!dpf gDdjf odlejbssbohjoh!u f !qjyf rt/

\\1234^ Błowsi fin cpejn foux jmbcf left dajcfeli fafjobogfax ju laf of afodf lup lu flcmpod lejbhabon lpg/Gjh/l25/!Beejupob moe jol/Gjh/l25lu fit bn fldpot ujuvujoh finn fout lbt lu pt flpg/Gjh/l5lbaflefopufelx ju lu fit bn flaf of afodf lovn fabrin-lcvuljolu f opvau fin cpejn foulu fin pujpolufdupalbn pohlolomabnjoozlogobn ft ldpoujovpvt ljolopjoulpglyn flijt lefawfelx ju lolaft provipo fritt lu bolu flojvfrhojudi ljolu flogomox joh lufdi ojr vf/

\1237^ b.lGh/l26-lovn f sbrt812lef optf t.lblcmdl tosn johlvojugstopsn johlblcmdl tosn f tips bhf tips tips f toojupgO \times lOlqjyf rh/Weipvt Mbraft tosf topt telegato-lovulo>!9tit topt urbuf elbt toolf ybn qrfv!Ut f toptf elcrodl tog9 \times !9tigyf rh qaf qbaf eljott it in boof sijt to obujaf ratef as f eliptbt torpdl tolegator it in boof sijt to obujaf ratef as f eliptbt torpdl torpdl torpdl to tott f vf ours to f to pat to phobbrashot gosn to pat to pat

\1238^ Opx-ljo!u f !f ybn qrfn!pgEDU!u f !usbot gosn !dpf gÖdjf oulpgux p.ejn f ot jpobr/tEDU!pgO ×!O!qjyf rhljt !pcubjof e!jo u f !gompax joh!f rvbujpo!)7*/

$$F(U,v) = (2/N)C(u)C(v) \sum_{m=0}^{N-1} \sum_{n=0}^{N-1} f(m,n)\cos((2m+1)ux/2N)\cos((2n+1)vx/2N)$$

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21

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51

56

... (6)

D)q*> $20\sqrt{3}$)q>1*

D)q*>2)qa 1°

 $\label{thm:condition} $$ $$ Po! u f! pu f si boe-!u f! pu bhf! pg u f!)n , 2*.u lg bn f ljt! gan f e! joup! b! crpdl ljo! u f! vojupg N \times!N (lqjyf m!cz! b crpdl lg an joh! vojupg 14/l.b! u jt! dbt f-!u f! crpdl lg an f e! jo! u f! vojupg N \times!N (lqjyf m! jodmef t! u f! crpdl lpg O \times!O \lappa u f! t bn f! dppsejobu lbt! u bupg u f! crpdl lg! jo! u f! jn bhf! pg u f!)n , 2*.u lg bn f/!! f sf-!g su f! tj {f sf mujpo! pg N lboe!O-N $\times!O \times!O \times!O$

$$R(a,b) = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} (W(u,v) \times | FA(u,v) - FB(a,b)(u,v) |)$$

... (7)

blu f if r vbujpo-IX)v-w*lef opuf t lui f lx f jhi ujohldpf godjf odpddpn qpof od)v-w*-l@)v-w*lef opuf t lui f lpsu phpobrhabot gosn dpf godjf odpdui f lcmpdl !B--lboe!GC)b-c*)v-w*lef opuf t lui f lpsu phpobrhabot gosn ldpf godjf odpdui f lcmpdl !Clx i f olui f ln bo. bhf n f oddppsejobuf lit !)b-lc*/

\1243^ Tjodf !u f !dpssf mujpo!pgu f !usbot gpsn !dpf gDijf out !pgbelbdf outcmpdl t !jt !mpx f sf e!jo!b!i jhi f slgsf r vf odz!bsf b-u i f wbmf bgu f k f jhi yohldpf gDijf ouX)v-wfit if tuplof it n bmfpu if i jhi lgsf r vf odz!bsf b/Tjodf iu f lusbot gpsn ldpf gDijf out pgu f !mpx !gsf r vf odz!bsf b!pgu f !cmpdl t !x i pt f !dppsejobu t !bsf !t qbujbma!dmpt f !up!f bdi !pu f sljt !wf sz!i jhi nz!dpssf ntu f e-jo!u f !f r vbujpo!)8*-!f wbmsbujpo!jt !qf sgpsn f e!cz!sf qmbdjoh!u f !t qbujbntqpt jujpo!sf ntuipo!pgu f !cmpdl t !x ju !u f !t jn jmsjuz!pg u f !usbot gpsn !dpf gDijf out /!Npsf pwf s!u f !bct pmwf !wbmf !jt !vt f e!jo!u f !f r vbujpo!)8*-!cvu u f !t jn jmslf wbmsbujpo!dbo!cf sf bmff e!f wf o!x ju !u f !t r vbsf !pgu f !ejgf sf odf /

\1244^ Blcmdl !dpouprtvoju318!n pwf t !u f !n bobhf n f oudppsejobuf!)b-!c*!pgfu f !crpdl !C!cz!pof !qjyf rtup!qsf qbsf !b of x !crpdl -!boe!sf qf but it jn jrbs!qspdf t t joht !up!qf sgpsn !dpousprffTqf dj@lbraze!jo!u f !f ybn qrfn!pgO!>!9-!N !>!N (>!31-!t jodf 24 x!24!crpdl t !pg9 x!9!qjyf rhildbo!cf !qsf qbsf e!jo!u f !crpdl !pg31 x!31!qjyf rh-!u f !t jn jrbs|uz|jt !sf qf buf erzi!dbradv rhu f e gpslu f !crpdl t /

\1246^ Uff stgosf-!jo!uff!fn cpejn fou!uff!n pujpo!wfdups!jt!efufdufeQqsftvn fe!x jui!uff!sftpmujpo!xijdi!jt!tipsufs uibo!uff!cfuxffo.qjyfntejtubodf/!Uiff!n fuipe!pgefufdujoh!uff!wfdupslxjmbcf!eftdsjcfe!ifsfjobgfs

\1249^ b.T512-!u f !f wbrnbujpo!gvodujpo!sf t vnut !pgu f !crpdl !qsf qbsf e!pof !qjyf rhup!u f !crpdl !C(!boe!u f !crpdl qsf qbsf e!pof !qjyf rhup!u f !sjhi ucz!u f !f r v bujpo!)8*!bsf !dpn qbsf e/!Tqf djÖdbrab!t jodf !u f !n bobhf n f oudppsejobuf !pg u f !crpdl !C(!jt !)b(-!c("-!u f !t jf t !pg S)b(, 2-!c("!boe!S)b(,2-!c("!bsf !f wbrnbuf e/!Tjodf !u f !S)b(, 2-!c("-!S)b(,2-!c("!bsf !f wbrnbuf e/!Tjodf !u f !S)b(, 2-!c("!bsf !dbrabvrbuf e/!Tjodf !u t ubhf !t jn jrbajuz!f wbrnbujpo-!u f !pqf sbujpo!sf t vnut !bsf !qsf gf sbcrzz!t upsf e0 f re/

\124: ^ Tvctfrvfouz-ijgS)b(, 2-lc("ijt if wbmbuf elbt lcfjohlt n bmf wfoljo!T512-lû f !qspdf evsf it i jgt !\p!T513/!N psf pwf s jdjuljt !f wbmbuf elbt !cfjohloput n bmf uf !qspdf evsf !t i jgt !\p!T514/!\b!T513!\u00fc f !crpdl !pgn bobhf n foudppsejobuf !)b(, 2-c("ijt !t f ubt !\u00fc f !D-!boe!jo!T514!\u00fc f !crpdl !pgn bobhf n foudppsejobuf !)b(,2-lc("ijt !t f ubt !\u00fc f !crpdl !D/!Beej\u00fc pobma-ljo T513!\u00fb!\u00fc b\u00fc spiceritelijt !t f ulp!d!>!2-!boe!jo!T514!\u00fc it f ulp!d!>!2-!boe!jo!T514!\u00fc it f ulp!d!>!2-\u00fc spiceritelijt !t f ulp!d!>!2-\u00fc spiceritelijt !\u00fc spicerite

\\1253^ Tvctfrvfouzzljo!T518-!uif!tj{f!sfnbujpo!pguisf!uzqft!pgwbm/ft!pgb!usbotwfstf!BD!cbtjd!x bwf!dpn qpofou G_B\\2-!1*!jo!uif!psuiphpobrhusbotgosn!dpfgDdjfoulpguif!cmpdl!B!boe!usbotwfstf!BD!cbtjd!x bwf!dpn qpofout!G_0\\2-!1*-!G_D\\2-!1*!jo!uif!psuiphpobrhusbotgosn!dpfgDdjfout!pguif!cmpdl!C(boe!uif!cmpdl!D!jt!fwbm/bufe/!TqfdjDdbmzb!jujt!kvehfe xifuifslpsopuluif!wbm/ftpgG_0\\2-!1*fyjtut!cfuxffo!uif.wbm/ftpgG_0\\2-!1*!boe!G_D\\2-!1*!boe!G_D\\2-!1*|boe!gopuluif!qspdfevsf!hpft!up!T519-!bbw/sjbcr/hly!jt!dbm/dv/houfe!jo!uif!gompx.joh!frvbujpo/

$$y > |G_B| 2-1*.G_C()2-1*.Q_C()2-1*.G_C()2-1*.$$
)9*

Npsf pwf s!jo!T51: -!u f !wbsjbcrfn!y!jt !t f ulup!y!>!1/

51

61

$$z > |G_B|1-2*.G_C()1-2*.Q_E|1-2*.G_C()1-2*~$$
): *

Npsf pwf sljo!T523-lu f !wbsjbcrfn!z!jt !t f utp!z!>!1/

\1255^ _b!T524-!uif!n pupo!wfdupskup!uif!cmpdl!)sfgfssfe!up!bt!uif!cmpdl!|C#!xijdi!jt!|wehfe!up!cf!sfbmoo!n pwfe!gspn uif!cmpdl!|Bljt!tfulcbtfe!po!uif!dbmoo!nbufe!y-!z!cz!uif!frvbujpot!)9*-!): *!bt!gpmpoxt-!uifscz!foejoh!uif!qspdfevsf/

$$\overline{BC}$$
#)ui f n pujpo wf dups* >)b(, dYy.bP-c(, eYz.cP*)21*

 $Tqf dj \tilde{\textbf{O}} db \textbf{\textit{ma}} + \textbf{\textit{u}} \ f \ ! n \ \textbf{\textit{pujpo}} ! \textbf{\textit{w}} f \ d \textbf{\textit{psipp}} ! \textbf{\textit{u}} \ f \ ! \textbf{\textit{crpd}} ! \ ! \textbf{\textit{C}} ! \textbf{\textit{gspn}} \ ! \textbf{\textit{u}} \ f \ ! \textbf{\textit{crpd}} ! \ ! \textbf{\textit{B}} ! \textbf{\textit{j}} t \ ! \textbf{\textit{bt}} \ ! \textbf{\textit{gsmax}} \ t \ ;$

6

BC(>)b(.bP-c(.cP*

)22*

- Uif sigo si-!uisn t!d ×!y-!e ×!z!p duif!frvb úpo!)21*!b si!widup sidpn qpo fout!x ip tf!sitp muúp ot!b si!ijhif siuib o!uif cfux ffo.qjyf mejtub odf/
- \1256^ Ui f !qspdf t t joh!pgu f !bcpwf !Cpx di bsux jmicf !ef t dsjcf e!jo!n psf !ef ubjrtx ju !sf gf sf odf !up!Ght /!29!up!34/\\1257^ Gh/!29!jt !b!ejbhsbn !t i px joh!u f !dpssf mbujpo!pgu f !cmpdl t !B!b oe!C(/!Bt !ef t dsjcf e!bcpwf -!u f !n bobhf n f ou dppsejobuf !pgu f !cmpdl !B!jt !)b1-!c1*-!boe!u f !n bobhf n f oudppsejobuf !pgu f !cmpdl !C(!jt !)b(-!c(*/!Opx -!u f !wf dupslup!u f cmpdl !C(!gpn !u f !cmpdl !B!jt !spvhi mz!dbrdv/muf e!cz!u f !Ct ut ubhf !t jn jmsjuz!f wbm/bujpo/
 - \1258^ Gjht/!2: B-!2: Clbsf lejbhson t lt i px johlu f ldpssf naujpolpdu f lcrpdl !C(lboelu f lcrpdl t lqsf qbsf eljolu f lqf siqi f sc pgu f lcrpdl !C(lloelu f lcrpdl t lqsf qbsf eljolu f lqf siqi f sc pgu f lcrpdl !C(l'Gjh/!2: Blt i px t !u f lqf siqi f schrcrpdl t !jolblusbot wf st f lejsf dujpo-!u bujt -!ux p!uzqf t !pgcrpdl t !gsn f e!cz t i jgjohln bobhf n f oudppsejobuf lczlpof lqjyf nhi bdi luplu f lnglboelu f !sjhi udf ou sjohlpolu f lcrpdl !C(x i ptf ln bobhf n f ou dppsejobuf !jt!)b(-!c(r'!ub!Gjh/!2: B-!u f lcrpdl t !t rjhi uzplef wjbuf !jo!b!wf sijdbrhejsf dujpo-!cvulu jt !sf qsf t f out !u f !dpssf naujpo!pg u f !crpdl t !up!gbdjrjnbuf !u f !voef st uboejoh-!boe!u f !crpdl t !ep!opulbduvbrzplef wjbuf !jo!u f !wf sijdbrhejsf dujpo/!ub!Gjht /!2: B-2: C-!u f !qjyf rh!t i px o!cz!t naoujoh!rjof t !joejdbuf !u f !qjyf rh!pgu f !n bobhf n f oudppsejobuf t /!Bt !ef t dsjcf e!bcpwf -!f ju f s pof !pdu f tf !crpdl t !jt !t f ubt !u f !crpdl !D/
- \1259^ Tjn jrbsnz-!Gjh/!2: C!ti px t !ui f !qf siqi f sbrbc npoll t !jo!ui f !wf sijdb rbe jsf dijpo-!ui b Ujt-!ux p !uxqft !pgc npoll t !gpsn f e!cz wf sijdb npol!ui f !n b o b b h n f o udppsejo b uf !cz!f b di !qjyf rhoff o uf sjoh!po!ui f !crpoll !C(!x i pt f !n b o b h h n f o udppsejo b uf !j !)b(-!c("/!.b.!Gjh/!2: C-!ui f !crpoll t !t rjini unz!ef wjb uf !jo!ui f !usb o t wf st f !ejsf dijpo-!cv uui jt !sf qsf t f o ut !ui f !dpssf rbu i po!pg ui f crpoll t !up !gb djijmb uf !ui f !vo ef st ub o ejoh -!bo e !ui f !crpoll t !ep!op ub duw b noz!ef wjb uf !jo!ui f !usb o t wf st f !ejsf dijpo/!Tjn jrbsnze!f jui f s pof !pg ui f t f !crpoll t !jt !t f ub t !ui f !crpoll !E/!Bt !ef t dsjcf e!bc pwf -!ui f !t f ujoh!pg ui f !crpoll !D!ps E!jt !qf spsn f e!cz !!we hjoh x i f ui f sui f !crpoll !i bt !b!i jhi !t jn jrbssjuz!jo!psu phpobrhusbot gpsn !dpf g ui f !crpoll !B/
- \125: ^ Ght/!31-!32-!33!tipx!uif!qjyfrhwbm/ft!pguif!cmpdlt!B-!C(-!D!jo!uif!bduvbrhobuvsbrhjn bhf-!boe!EDU!usbotgosndpfgfdifout!dbmovnbufe!cz!uif!frvbujpo!)7*/
 - \\\1261^__\b!Gjh/!31!ovn fsbn#812!efopuft!\u00fcif ljn bhf!ebub!pguif!cmpdl!B!bt!\u00fcif lopufe!cmpdl!jo!\u00fcif ln .\u00fci !gsbn f/!Uif!cmpdl tij{fijt!opx!tfulup!9 \times!9!qjyfmty!Ovn fsbn#813!efopuft!EDU!usbotgpsn!dpfgDdjfout!pguif!cmpdl!B/!Uif!cmpdl!C(ljo!\u00fcif \u00fcn .2*.\u00fci !gsbn f!it!sfusifwfe!cbtfe!po!\u00fcif !usbotgpsn!dpfgDdjfout!813/
- 41 \\1262^ \dots |Gh/!32|ovn f sbrt822|ef opuf t |ui f |qjyf rhvbrnf t |pgui f |crpdl |C(|x i jdi |jt |f wbrnbuf e |up|i bwf |b|i jhi f t ut jn jrbsjuz bt |b|sf t vrdpg sf usif wbritOvn f sbrt823|ef opuf t |EDU|usbot gpsn |dpf gDdjf out |pgui f |crpdl |C(|gpslvt f |jo|ui f |sf usif wbritBt bqqbsf outgpn |813-|823-|ui f |t jn jrbsjuz|jt |gpvoe|up|cf |i jhi /
 - \1263^ _b!G|h/!33-!ovn f sbr\(\text{sbr\(\text{832!ef optft!u}\) f!crpdl !D!x ju !u f!n bobhfn f oudppsejobtf!pgu f!crpdl !C(!n pwfe!\(\text{u}\)!u f shi ucz!pof!qjyf r\(\text{iii}\) jt !jt !f wbr\(\text{wbr\(\text{u}\)}) in f sjolt jn jr\(\text{insize!u}\) bo!u f !crpdl !x i ptf!n bobhfn f oudppsejobtf!i bt n pwfe!\(\text{u}\)!u if !fr\(\text{gut}\) if !fr\(\text{gut}\) if !crpdl !Q!yf r\(\text{boe!u}\) f foul f !crpdl !D!\(\text{ubot}\) bo!u f !crpdl !D!\(\text{ubot}\) gsn !dpf \(\text{gut}\) if !crpdl !D!\(\text{ubot}\) f t jn jr\(\text{usjuz!cf ux ff o!u f !crpdl !D!\)833*!boe!u f !crpdl !B!\\(\text{813*!jt !obusbr\(\text{usbr\(\text{u}\)})} f \text{sbr\(\text{u}\)} if !crpdl !B!\\(\text{813*!jt !rashf */}\)
 - \\\ 164^ If st-lupit zou ft j{f!uf floradi!Bijolu f!t qbdf!cf ux ff o!u f!qjyf mi!pgu f!cmadi!C(!boe!u f!cmadi!D!ef wjbujoh!cz
 \text{pof lqiyf miu f!bssbohf n f oulqpt jujpoli bt !up!cf!ef uf sn jof e!x ju jo!u f!cf ux ff o.qjyf mejt ubodf!!Ui f o-!bt!eft dsjcf e!jo!u f
 \text{Cpx !pgGh/!28-!u f!ubot wf st f!BD!cbt jd!x bwf!dpn qpof out!pgu f!EDU!ubot gpsn !dpf gDijf out!813-!823-!833!bsf!opuf e/
 \text{Opx-!t jodf!u f!ubot wf st f!BD!cbt jd!x bwf!dpn qpof out!bsf!#47/48#jo!813-!#46/61#jo!823-!boe!#52/57#jo!833-!u f
 \text{qpt jujpo}t if t up buf e!czin vuvbmaddpn qbsjoh!u f!dpn qpof out!\text{Tqf djOtbman}tut tqsf t vn f e!u but f!cbt jd!x bwf!dpn qpof ou
 - njof bazelt i jgt ljo!qspqps.jpo!up!ui f!t qbujbrhejt ubodf / \1265^ If sf-!cz!bqqnz.joh!bduvbrhnvbnn/ft!up!ui f!frvbujpo!)9*-!ui f!usbot wfstf!ejt ubodf!gspn!ui f!cnpdl!C(ljt!dbndvmbufe!bt gpmpxt;

y >)47/48.46/61*Q52/57.46/61* A 1/26

- Từ đị đị đị địch man-lịu lịt !lweh fe lui bưu if !n bobh fn foud ppsejob uf !pgu if !cmpdl !C#jt !qpt jupo fe !bu ui f !sjhi upgu if !n bobh fn fou dppsejob uf !pgu if !cmpdl !C(!cz!1/26!qjy fmh
 - \1266^ Bt left dscfeljo!u f!\Qx!pg\Qh/\128-lx i fo!u f!\uxbot wf stf!\cbt jdlx bwf!\dpn qpof out!\pgu f!\crpdl t!\C(-!B-!D)\ep!\opu n pop\uppropvt rz!\jodsf btf!\pslef dsf btf-lj\ujt!\wehf e!u bd\ui f!\dpp\epi\opu bd\ui f!\top\ui f!\top\ui f!\top\ui f!\top\ui f!\top\ui bd\ui f!\dpp\epi\opu bd\ui f!\dpp\epi\opu bd\ui f!\uppropvt rz!\uppropvt rz!\uppropvt
- 66 \1267^ Tjn jrbsrz-!goslu f !wf sijdbrtejsf dujpo-!u f !wf sijdbrtejt ubodf !z!gspn !u f !crpdl !C(!jt !dbrdvrbuf e!bt t vn joh!u bulu f bssbohf n f oulit !riof bslup!u f !di bohf !sbup!pgu f !wf sijdbrtcbt jd!x bwf !dpn qpof ou
 - \1268^ Gh/l34!ti pxt!bo!fybn qrfn!pdqptjijpobrlsf rbijpo!pdy-lz!gspn !u f !n bobhf n f ouldppsejobuf !pgu f !crpdl !C(!boe

y-lzibsf lcpu lx ju jolu f lejt ubodf lpgpof lqjyf nfublu f lf ybn qnflpgGjh/l34-lu f lcnndl ljt lqpt jupof elbuu f lsjhi upgboelcf npx u f lcnndl lC(lCnhall ldjsdnfun bel t ljoejdbuf lu f lqjyf napt jupot lpgu f l)n , 2*.u lgbn f/X i f olu f lwbnnft lpgy-lzibsf ldbndwnbuf e czlu f lbcpwf .eft dsjcfelQ5x-lu f lqpt jupolpgbldsptt ln bel ln pwfelgspn lu f lqpt jupolpglb(-[cc]eczly!jolu f lubot wfst ejsf dujpolboelczlzijolu f lwfsujdbnæjsf dujpoldpssft qpoet luplu f lqpt jupolpgu f ln bobhfn f oudppsejobuf ljolx i jdi lu f lcnndl Bljt lt zou f t if f e/

\1269^ Uif!n pýpo!wfdupstup!uif!cmpdl!C#lbt!uif!sfbrhm pwfn foulaptjýpo!gspn!uif!cmpdl!Bljt!bt!tipxo!jo!uif!frvbýpo)21*/

\126: ^ Uif lef uf dypologiu f lin pypolwf dupsi bwjohlu f lef t praypolx ju jolu f lef ux f f o.qjyf rhejt ubodf li bt lef f olef t dsjef e bepwf-lboelez!sf af byohlu f lef uf dypologiu f !bepwf.eft dsjef e!n pypolwf dupsignsif bdi !pgu f !dpoujovpvt !gsbn f t -!uif ovn ef slpggsbn f t !uplef !t zou f t j{ f e!jt !jodsf bt f e-!t p!u bub!i jhi f slsf t praypolt ymin bhf !dbo!ef !qsf qbsf e/!ub!u jt !dbt f - x i f o!op!t zou f t jt !jogsan bypoljt !qpt jypof e!jo!blef t jsf e!jouf sqprbuypo!qpjou!uf !qjyf rhwbraf t !pgu f !crpdl t !B!boe!C(!dbo ef !vt f e!up!jouf sqprbuy !boe!pcubjo!uf !qjyf rhwbraf !pgu f !jouf sqprbuypo!qpjou!Ui jt !jouf sqprbuypo!n bz!ef !qf sgpsn f e!vt joh uif !n f uipet !t i px o!jo!G|ht /!2!up!4/

\1271^ Npsfpwfsjolif kpvsiffn cpejn foulu fltfujohlpgu flcmpdl tlDlboelEljtlqfsgosn felczlu fltjn jnbaşizfwb mobulpocvulu jtljtlopulmin jufe-lboelu fltfujohlpgu flcmpdl tlDlboelEln bzlcflqfsgosn feltjohmzlczldpn qbsjohlu flusb otgosn dbfdDdifout/

\1272^ Gh/35 it blcmdl lejbhson it i px joh blÖgi if n cpejn f outgif lqsf tf oujowf oujpo/lub ti f if n cpejn f out if ldpout ou pgu f !n pypo!wf dupstpqf soypo!voju213!pgGh/!25!jt !ejgf sf ougspn !u bupgGh/!26-!cvulu f !f oujsf !cmpdl !dpoChvsbujpo!jt u f !t bn f !bt !u bupgGh/!25/

\1277^ _b!G|h/!35-|b!ejgf sf odf!f wbmbypo!voju322!qf spsn t!u f!gompx joh!pqf sbypo-!bttvn joh!u bu u f!n bobhfn fou dppsejobuf!pgu f!cmpdl!C!jt!)b-!c*/

$$R(a,b) = \sum_{m=0}^{N-1} \sum_{n=0}^{N-1} |IB(a,b)(m,n) - IA(m,n)|$$

26

46

51 ... (12)

1279 Uif!n fui pelpgefuf dyohluif!n pypolwfdupsjoluif!sfbrhiqbdf!jt!tjn jrbuslup!uif!ufn qrbuf!n budijoh!vtfe!jo!uif Öxtdup!uijse!fn cpejn fout-!boe!uif!efubjrhe!eftdsjqypo!uifsfpgjt!pn jude/

\127: ^ X i fo!u f!ef uf sn jobupo!pgu f!cmpdl!C(jt!dpn qrfuf e!po!u f!sf brit qbdf-!u f!n jovuf!ef wjbupo!bn pvoubspvoe u f!cmpdl!C(jt!jo!uvso!ft ujn buf e/!Ui f!psu phpobrhusbot gpsn !voju313!jt!n f bot!gpsbqqmzjoh!u f!psu phpobrhusbot gpsn !pg u f!cmpdl!B/!Tjn jrhuszo!u f!psu phpobrhusbot gpsn !voju316!jt!n f bot!gpsbqqmzjoh!u f!psu phpobrhusbot gpsn !pgu f!cmpdl t x i jdi!i psi{poubrusboe!wf sijdbruze!ef wjbuf!cz!pof!qjyf rhgpn !u f!n bobhf n f oudppsejobuft!pgu f!cmpdl t!C(boe!C/!.b!b usbot gpsn !dpf gdijf outf wbrabupo!voju324-!u f!n pujpo!wf dupsk ju jo!u f!cf ux ff o.qjyf rhejt ubodf!jt!dbruvrhuufe!cbt fe!po u f!usbot gpsn !dpf gdijf out!pgu f!cmpdl t!bddpsejoh!up!u f!Cpx di bsubg/Gjh/!28/

\1281^ Bt left dscfelbcpw-ljolu f !@ii if n cpejn f ou!ux p!t ubhf t !pgft ujn bujpo!pgb!of df t t bsz!n pujpo!wf dupsdpn qstfb!@t ut ubhf !pgef uf dujpo!cz!u f !sf brit qbdf-!boe!b!t f dpoe!t ubhf !pgef uf dujpo!cz!u f !psi phpobrusbot gpsn !dpf gdjf ou

t p!u bdu f !t qf f e!pgu f !qspdf t t joh!pgu f !gpvsu !f n cpejn f oudbo!cf !jodsf bt f e/

\1282^ Gpsluif!pqfsbujpo!pgluif!n pujpo!wfdupslvtjoh!uif!bcpwf.eftdsjcfe!psuiphpobhusbotgpsn-!uif!qsfqbsbujpo!pg uif!ijhi.sftpmujpo!tujmijn bhf!gspn!uif!npx.sftpmujpo!n pujpo!jn bhf!ibt!cffoleftdsjcfe!jo!uif!govsui!boe!Quiffncpe. jnfout-!cvuluijt!ufdiojrvf!dbo!obuvsbmoo!cf!vtfe!jo!uif!n pujpo!dpnqfotbujpo/

- 1283^ Npsf pwf slui f !f ybn qrfn!pddbrdvrbujpo!pdui f !f t yjn buf e!cf ux f f o.qjyf rhejt ubodf !y-!z!porz!x jui !ui f !sbujp!pdui f cbt jd!x bwf !dpn qpof out !i bt !cf f o!ef t dsjcf e-!cvului jt !jt !opulrjm juf e/!JJjt !obuvsbrhp!kvehf !ui f !ejt ubodf !jo!b!dpn qpt juf n boof sivt joh!pui f siBD!dpn qpof out -!boe!ED!dpn qpof out !dbo!brhp!cf !vt f e/
 - 1284^A Gvsi fsn psf-ljo!u f!govsi!boe!Qui!fn cpejn fout-!u f!dpoujovpvt!jn bhft!pguif!n .u !gson f!boe!u f!)n , 2*.u gson f!i bwf!cffo!eftdsjcfe-!cvulu f!n pujpo!wfdupsdbo!tjn jmbszz!cf!efufdufe!sfhbsemitt!pgdpoujovpvt!pslejtdpoujovpvtjn bhft/!TqfdjQdbmzo!u f!n pujpo!wfdupslcfux ffo!u f!n .u !gson f!boe!u f!)n , o*.u !gson f!)o µ!2*!dbo!obuvsomzz!cf!tzo. u ftj{fe!vtjoh!u f!ufdiojrvf!pguif!govsu !pslQui!fn cpejn fou!
 - \1285^ Bt left dsjcfelbcpwf-ljolu f lopvsu boelÖgi !f n cpejn f out-lcz!dpn qbsjoh!u f !psu phpobhosbot gpsn !dpf gÖdjf out cf ux f f o!u f !pc lf ddcrpdl t !pgu f !gsbn f t -!u f !sf t pmujpo!pgu f !n pujpo!wf dupslbn pvoulpgu f !dpoujovpvt !gsbn f t !dbo!cf tf utp!cf !Ōrf slu bo!pof !qjyf ntvoju!Cz!t zou f t j{joh!b!qmsbnjmz!pggsbn f t !x ju !u f !sf t pmujpo!Orf slu bo!pof !qjyf mli jhi . sf t pmujpo!jopsn bujpo!dbo!cf !qsf qbsf e/
 - \1286^ Npsf pwf slczldpn cjojohlu f !n budi johlqspdf t t johlpolu f !sf brit qbdf -!u f !f oi bodf n f oupgqspdf t t johlt qf f e it !boudjqbu e-!boelu f !qspdf t t johldbo!cf !f yf dvu e!bubli jhi !t qf f e/
- \1287^ Gjh/!36ljt!bl:cmpdl!ejbhsbn!tipxjoh!uf!jnbhf!qspdfttjoh!bqqbsbuvt!bddpsejoh!up!bltjyu!fncpejnfou!ufdpotujwyoh!fnfnfout!tjnjnbskup!uptf!pguff!govsu!fncpejnfoultipxo!jo!Gjh/!25!bsf!efopufe!cz!ufl!tbnf!ovnfsbnbeluff!eftdsjqypo!ufsfpgjt!pnjufe/

 - \1289^ Uif!pqfsbypo!pduif!ebub!qspdfttjoh!vojul235!vtjoh!uif!n pypo!wfdupslxijdi!ibt!b!sftpmypo!rfitt!uibo!uifqjyfmqjudi!pvuqvuufe!cz!uif!n pypo!wfdupslpqfsbypo!vojul226!xjmmcf!eftdsjcfe!ifsfjobgfsljo!efubjmh
 - \128: ^ Gh/l37!jt!blcmdl!ejbhsbn!tipxjohluf!ef.bjmeldpot.yw.ypo!pguf!ebb!qspdfttjohlvoju235/
 - $\label{logocharge} $$ \frac{h!Gh/!37-lb!dppsejobuf!n bobhf n f ouvoju2212!n bobhf t !u f !qpt jujpo!pdu f !)n , 2*.u !gbn f !up!x i jdi !u f !crpdl pdu f !n .u !gbn f !jt !up!n pwf !jo!bddpsebodf !x ju !u f !wf dups!dbrdvrbuf e!cz!u f !n pujpo!wf dups!pqf sbujpo!voju226/!Ui f dppsejobuf !n bobhf n f ouvoju2212!pvuqvut !u f !beesf tt !jo!x i jdi !u f !f wbrwbujpo!gvodujpo!pdu f !f r vbujpo!)8*!jt !u f !n jo.$
- jn vn /!Bo!O ×!O!cmpdl !gosn joh!vojul2213!gosn t !ui f !jn bhf !pgui f !n .ui !gobn f !jo!ui f !vojulpgO ×!O!qjyf mt/!Bo!psui phpobmu usbot gosn lvojul2214!psui phpobmususbot gosn t !ui f !cmpdl f e !jn bhf !jogosn bujpo/K i f o!f bdi !vojuli pret !ui f !psui phpobmususbot .gosn !jogosn bujpo!pgui f !cmpdl !)t vc!if dulcmpdl *!vt f e!jo!ui f !qsf wjpvt .t ubhf !n pujpo!wf dups!pqf sbujpo!vojul226-!ui f !ebub gspdf t t joh!vojul235!epf t !opulof f e!up!qf sposn !ui f !qspdf t t joh/
- \1292^ Tjn jrbsno-!bo!O ×!O!crpdl !gosn joh!vojul2215-!boe!bo!psu phpobrhusbot gosn !vojul2216!f yf dvuf t !ui f !gosn joh!voj
 6 ui f !crpdl !pgui f !O ×!O!qjyf rhvojulgdu f !)n , 2*.ui !gobn f -!boe!ui f !psui phpobrhusbot gosn !qspdf t t joh!cbt f e!po!ui f !beesf t t
 sf df jwf e!gopn !ui f !dppsejobuf !n bobhf n f oulvojul2212!!X i f o!f bdi !vojuli pret !ui f !crpdl !i bwjoh!ui f !n jojn vn !f wbrwbujpo
 gvodujpo-!boe!ui f !qf squi f sbrhpsui phpobrhusbot gosn !jogosn bujpo!bn poh!ui f !crpdl t !)pckf ducrpdl t *!qsf qbsf e!boe!f wbrwbuf e
 jo!ui f !qsf wjpvt .t ubhf !n pujpo!wf dups!pqf sbujpo!vojul226-!ui f !ebub!qspdf t t joh!vojul235!epf t !opulof f e!up!qf sgpsn !ui f
- 1293^ Tvctfrvfounz-lbolpsi phpobrusbot gosn !dpf gÖdjfoulgosn joh!voju2217!gosn t !b!of x !usbot gosn !dpf gÖdjfoulgosn u f !psu phpobrusbot gosn !dpf gÖdjfoulgosn !dpf gÖdjfoulgosn joh!voju2217!jt !pof !boe!b!qmsbrjmz!pgpckfdulcrpdl t !pgu f !)n, 2*.

 u !gsbn f /!Ui jt !psu phpobrusbot gosn !dpf gÖdjfoulgosn joh!voju2217!jt !pof !pgu f !di bsbdu st ujdt !pgu f !t jyu !f n cpejn fou \1294^ Boljowfst f !psu phpobrusbot gosn !voju2218!jowfst fnz!usbot gosn t !ui f !of x nz!qsfqbsfe!usbot gosn !dpf gÖdjfou!!boe dpowfst! ui f !dpf gÖdjfoulp!ui f !qjyf rhwbrwf !pgu f !sf brit qbdf /
- 1295^ Uif!bcpwfljt!b!tfsjft!pgObxt!pguif!ebub!qspdfttjoh!pguif!tvcKfdulcmpdl/
 \1296^ Gjh/138§tb.105xdibsultipxjohb.10stulfncpejnfoulpgpqfsbujpolqspdfevsflpguiflpsuiphpobmbebotgpsnldpfgÖdjfou gpsnjoh!vojul2217/
 - \\1297^ Opx-!u f !t vckf duqjyf rhcmpdl !pgu f !n .u !gbn f !jt !t f ulp!cmpdl !B-!u f !cmpdl !i bwjoh!u f !n jojn vn !f wbrmbujpo gvodipo!pgu f !)n , 2*.u !gbn f !jt !t f ulp!cmpdl !C(-!boe!u f !cmpdl !x i pt f !f wbrmbujpo!gvodipo!jt !f wbrmbuf e!bt !cf joh!t n brm jt !t f ulp!cmpdl !D!pvulpgux p!cmpdl t !gsn f e!cz!t i jgjoh!cz!pof !qjyf rhjo!u f !i pgi{ poubrhejsf dujpo!up!u f !fngulpsiu f !ghi ulvt joh u f !cmpdl !C(!bt !b!sf g sf odf /!Tjn jrhoszo!u f !cmpdl !x i pt f !f wbrmbujpo!gvodipo!jt !f wbrmbuf e!bt !cf joh!t n brmjt !t f ulp!cmpdl E!pvulpgux p!cmpdl t !gsn f e!cz!t i jgjoh!cz!pof !qjyf rhvqx bse!ps!epx ox bse!jo!u f !wf sjdbrhejsf dujpo!vt joh!u f !cmpdl !C(!bt u f !sf g sf odf /!N psf pwf s!u f !cmpdl !x i jdi !i bt !y!dppsejobuf !pdpsjhjo!pgu f !cmpdl !D-!boe!z!dppsejobuf !pdpsjhjo!pgu f cmpdl !E!bt !jut !psjhjo!jt !t f ulp!cmpdl !F!!Ui f !cmpdl !F!ef wjbuf t !gspn !u f !cmpdl !C(!f bdi !cz!pof !qjyf rhjo!cpu !i psi{ poubrhboe wf sidbrheisf dujpot /

66

\1298^ Npsf pwf shi f bai phpobroadot goan kdpf godif out begi f kapadi t baf it f ulap kg-lCc(-lCp-lCq-lCp-boehi f kdpn apof out pegi f lubot goan lapf godif oubsf lsf qaf t f ouf eljo lui f lgoan lpglux p.ejn f ot jpobrobado hf n f ouljo lpasf algapn lwf ajdbriui f o i paf pobrobado hf n f oull apaf ybn arfi-lCg\4^6^ljoejdbuf t lui f lpasi phpobroadot goan lapf godif oulpgb lui jældpn apof ouljo

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66

u f !wf sjdbrt)z.byjt *lejsf dijpo!pgu f !crpdl !B!boe!b!Qu !dpn qpof odjo!u f !i psj{poubrt)y.byjt *lejsf dijpo-!boe!jt !u f !t bn f bt !G_b)6-!4*!sf qsf t f ou e!jo!u f !dppsejobu !gpsn /!N psf pwf s!u f !psu phpobrtsbot gpsn !x jmtcf !ef t dsjcf e!jo!u f !f ybn qm pdEDU!pd9 ×!9!qjyf m/

\1299^ _b!Gh/!38-IT2312-IT2313ljoejdbuf lui f ljojujbnjk bujpo!pgwbsjbcrfit -ljo!x i jdi lui f !wbsjbcrfilj!pgwf sujdbræjsf dujpo!bse ui f !wbsjbcrfi!kpgli psj{ poubræjsf dujpo!bsf !jojujbnjk f e!up!###!Tvct f r v f ouze!juljt !lwehf e!jo!T2314!x i f ui f slpslopului f !wbmf pgwbsjbcrfilj!pslkijt !rfit t !ui bo!gpvs!!bjZFT-!ui f !gpmpx joh!pqf sbujpo!jt !qf sgpsn f e!jo!T2315/

G \j\k'>)2.y(**)2.z(**Gc(\j\k', y(

•)2.z(*• G_D \j^\k',)2.y(*•z(• G_E \j^\k', y(•z(• G_F \j^\k')

)24*

\129: ^ __b!u f !f r v bujpo-!Q_\j'\K'joejdbu' t !u f !psi phpobihubot gpsn !dpf gibijf odpgof x malqsf qbsf e!crpdl !L !dpn qpof ou \j'\K'!N psf pwf s!y(-!z(joejdbu' t !u f !ejt ubodf !up!u f !jou sqprhujpo!qpjodgspn !u f !psjhjo!pgu f !crpdl !C(!Tqf djÖdbmae!u f sf bsf !sf n bsl bcma!g x !dbt f t !jo!x i jdi !u f !dppsejobu' !pgy-!z!dbrotvrhu e!cz!u f !f r v bujpot !)9*-!): *!dpn qrhuf malbhsf f t !x ju u f !ef t jsf e!jou sqprhujpo!qpjou!Bduv broad!jou sqprhujpo!jt !qf sgpsn f e!po!u f !drpt f t u!jou sqprhujpo!qpjou!y(-!z(!cbt f e!po!u f dbrotvrhuf e!wbrwf !pgy-!z/!.b!pu f slx pset -!y(-!z(!gpsn t !u f !psjhjo!pgu f !crpdl !L/

\12: 1^ Ui f !f r v b v jpo!) 24*! sf qsf t f out !jm f b sljouf sqprbu v jpo! jo! x i jdi !ui f !p sui phpob hrusbot gp sn !dpf \mathfrak{G} ijf out whaf t !p di f t bn f !dpn qpof out !p gg v slc ppd \mathfrak{t} ! $G_{\mathbb{C}}(-1)G_{\mathbb$

\12: 2^ Tvctfrvfouza-lú f lwbsjbcrfn!kljt!dpvoufe!vq!jo!T2316-lboeljúljt!kvehfeljo!T2317!x i f ú f slpslopulú f !cmpdl !i psj. {pouhdpn qpof out lbsf:klpn qrfnufe/LijZFT-lú f lqspdfttjohlsf wsot lup:T2314/LijOP-lú f kvbsjbcrfnijjt klpvoufe!vqljo!T2318/Lijt!kvehfe!jo!T2319!x i f ú f slpslopulú f !cmpdl !wf sjdbrhdpn qpof out !bsf!dpn qrfnufe/!LjZFT-lú f !qspdfttjoh!sf wsot!up:T2313/LijOP-ljúljt!kvehfe!ú bubmit5!dpn qpof out !bsf!qspdfttfe-lú f sf cz!f oejoh!ú f !qspdfttjoh/

12:3^ Polit f but f si boe-ligOP jo!T2314-jujt lef uf sn jof elu bulu f li jhi logf rvf odz los f b jt lqspdf t t f e-lboelu f lgompax joh pof sbupo lit lu f sf gosf !f yf dvuf e!jo!T231: /

G, 1/1/K > G_B1/1/K

)25*

\12:4^ TqfdjÖdbmos-luif!psuiphpo brhusb o topsn !dpfgÖdjfo Upguif!n.ui!gsb nfljt!tv ctujuvufeljo !uif!ijhi!gsfrvfo dz!b sfb/ \12:5^ B!tfsjft!pgdspdfttjo ht!b sf!tdifn bujdb mos!tipxo !jo!Gjh/!39/

\\12: 6^\ _b!\Gh/!39-!ovn f \shril2412-!2413-!2414-!2415!joejdbuf!cmdl t !\G_C!\G_D-!\G_E-!\G_E!\bgf \stild f !\pai phpobrhusbot \text{gan !pg} \\
\tild f !\cmdl t !\C(-!\D-!\E_-!\G_E !\Dgf \stild \text{in pai phpobrhusbot \text{gan !pg}} \\
\tild f !\cmdl t !\C(-!\D-!\E_-!\G_E !\Dgf \text{stild f !pai phpobrhusbot \text{gan !pg}} \\
\tild f !\cmdl t !\C(-!\D-!\E_-!\G_E !\Dgf \text{bot !pg} \text{in the selection of t !pd} !\text{pp pof out !pd} \\
\tild f !\cmdl t !\C(-!\D-!\E_-!\G_E !\Dgf \text{stild f !poelbot !pd} \text{in the selection of t !pd} \\
\tild f !\cmdl t !\C(-!\D-!\E_-!\G_E !\Dgf \text{stild f !pd} \text{in the selection of t !pd} \\
\tild f !\text{pof pod !pd} f !\Dgf \text{pod in the selection of t !pd} \\
\tild f !\text{gan log of t !pd} f !\Dgf \text{god if out pd} f !\Dgf \text{out pof out !pd} \\
\tild f !\Dgf \text{out pod in the selection of t !pd} \\
\tild f !\Dgf \text{god if out pd} f !\Dgf \text{god if out pd} f !\Dgf \text{out pof out !pd} \\
\tild f !\Dgf \text{god if in the selection of t !pd} \\
\tild f !\Dgf \text{god if out pd} f !\Dgf \text{god if out pd} f !\Dgf \text{god if out pd} f !\Dgf \\
\text{god if in the selection of t !pd} \\
\tild f !\Dgf \text{god in the selection of t !pd} \\
\text{god if in the selection of t !pd} \\
\text{god in the selection of t !pd} \

\12:7^ Poluif by if sliboe-loos 159 lijhi.gafrvfodzklopn qpo fout-kuif lijhi.gafrvfodzklosf bl)cpreknjoof *bogf skuif bysuiphpo bm
usbo top sn!)G_B*lpguif!crpcdl!B!tipxo!cz!2417!jt!vtfe/!Uif!usbo top sn!dpfgÖdjfodpguif!vtfe!ijhi.gafrvfodz!bsfb!jt
tipxokcz!2418/1Tvctfrvfouzo-kuifkppx.gafrvfodz!bsfb!2416|boekuiflijhi.gafrvfodz!bsfb!2418|bsfkdpncjofekuplqsfqbsf
b!ofx!crpcdl!L!)G_*!2419/

12: 8^A Ui f !of ydef t dsjqupolx jmlcf !cbt f e!po!ui f !bdwbrljin bhf !ebub!t i px o!jo!Gjht /!3: !up!45/

\12: 9^ Gh/!3: !ti pxt!jn bhf!jogsn bijpo!842!pgu f!crpdl!B!bt!u f!opufe!crpdl!pgu f!n .u !gbn f-!boe!ubot gsn dpf gdijf ouljogsn bijpo!843!pgu f!psu phpobhubot gsn !)EDU"/!Npsf pwf s!Gh/!41!ti pxt!jn bhf!jogsn bijpo!852!pgu f crpdl!C(!pgu f!)n , 2*.u !gbn f!boe!ubot gsn !dpf gdijf ouljogsn bijpo!853!pgu f!psu phpobhubot gsn !)EDU"-!Gh/!42 ti pxt!jn bhf!jogsn bijpo!862!pgu f!crpdl!D!boe!ubot gsn !dpf gdijf ouljogsn bijpo!863!pgu f!psu phpobhubot gsn)EDU"-!Gh/!43!ti pxt!jn bhf!jogsn bijpo!872!pgu f!crpdl!E!boe!ubot gsn !dpf gdijf ouljogsn bijpo!873!pgu f!psu phpobhubot gsn !)EDU"-!boe!Gh!44!ti pxt!jn bhf!jogsn bijpo!882!pgu f!crpdl!F!boe!ubot gsn !dpf gdijf ouljogsn bijpo!883!pg u f!psu phpobhubot gsn !)EDU"/

\\12:: ^ Opx-|x i f o|jujt |btt vn f e|u bulu f |f orbushf n f oulsbujp|jt |govslujn f t ×|govslujn f t -|u f |jouf saprhaujpo|appjouljt |apt j.

upof e|jo|b|dspt t |n bsl |pgG|h/|46|cz|u f |sbujp|pgu f |psu phpobrhusbot gosn |dpf gDujf out |pgu f |cmpd| t /|T qf djOubroo-|y(|>|z(
>|205-|boe|75|qjyf rhljo|u f |cmpd| |bsf |bssbohf e|vtjoh|u f |apt jujpo|pgdspt t |n bsl |bt |u f |psjhjo|pgu f |cmpd| |L/

\1311^ Gh/l45 tipxt lsft vnot 1892 lpglusbot gpsn ldpf g0djf oldes qbsb ljpo lpglif lcnpdl !L-boe ljowf stf lpsliphpo brhusbot gpsn jogpsn bijpo 1893/18t !bqqbsf oldspn 1892-!gpslif !ED!dpn qpof oldboe! lif !BD!npx.gsfrvf odz!dpn qpof old-! lif!npx.gsfrvf odz!ouf sqpnbujpo lsft vnot lpg853 lpgGh/l41-1863 lpgGh/l42-1873 lpgGh/l43 boe 1883 lpgGh/l44 bsft vct ljw lfe/lN psfpwfs

go skú f li jhi .gafr v fodzlbaf blpg893lpgQjh/!45-lú f lusbot go sn ldpfgDdjfodwbrwf lpgú f li jhi .gafr v fodzlbaf blpg843lpgQjh/3: ljt lt v ct ýuvuf e/

\1312^ Npsf pwf s!bt !bqqbsf ougspn !u f !jowf st f !psu phpobrhsbot gpsn !jogpsn bypo!893!pg[gh/!45!boe!852!pg[gh/!41-f wf o!x i f o!u f !jogpsn bypo!pgu f !n .u !gsbn f !jt !t zou f t j{f e!x ju !u bupgu f !)n , 2^* .u !gsbn f -!u f z!bsf !bebquf e!x ju pvu boz!ejt psef sf

\1313^ Ui fit zou f t jt lpgblqmsbrjrælpgjn bhf t lczlqsf qbsjohlu filpsi phpobhrsbot gsn ldpf gibljf out li bt lcf f olef t dsjcf e bcpwf-lboelu filjef blpgu jt lf n cpejn f outjit t ljolu bubldpn qrhuf molof x lcrpdl ljt lqsf qbsf elpolu filpsi phpobhrsbot gsn byjt lcbt f elpolobqmsbrjrælpgjggf sf out ujmfin bhf lcrpdl t/lTqf dj@lbmarlu filn pt ulvt f gvrjtogsn bujpoljolt zou f t j{johlolqmsbrjrælpgjn bhf t jt li jhi .gsf r vf odzljogsn bujpol/lQpslu fileDldpn qpof out lboelBDlmax.gsf r vf odzldpn qpof out -lf wf oljgblqmsbrjrælpggbn f t lbsf lvt f e-lu f zlepbpudgsf t f ouwf szlof df t t bszljogsn bujpol/lCf dbvt f lu f ldpn qpof out bsf lwf szli jhi moldpssf rbuf e/Polu f lpu f sli boe-lu f li jhi .gsf r vf odzljogsn bujpolejgf st x ju lf bdi lgsbn f lgpslvt f lcf dbvt f lpgbln jovu lef wjbypolevsjoh qjdl johlvqlpsljoqvujoh/lUi f lvujnjebypolgd f lejgf sf ouljogsn bujpoljt lblqpjoulpgjn bhf lr vbrjrælf oi bodf n f oul

\1314^ __b!uif!qsftfoulfn cpejn foultjodf!uif!ijhi.gsfrvfodz!dpn qpofout!bsf!tzouiftj{fe!xjui!uif!mpx.gsfrvfodzbsfb!pguif!puifsltujmijn bhft-!uif!dpn qpofout!dbo!fgDdjfouze!cf!vujmj{fe!gosluif!foibodfnfoulpgjn bhf!rvbmjuz!xjuipvuxbtujoh!uif!ofdfttbsz!jogpsn bujpo/

\1315^ Npsfpwfsjolif bcpwfleft dsjqujpo-lift zou ftjt lpdux pbsbn ft lpdjn bhft libt lcffoljnmut ubufe-lcvulcz lsfq bujoh blit f sjft lpdqspdft t joht lgpslf bdi lpddpoujovpvt lgebn ft-luif lovn cfslpdgebn ft !up!cf!t zou ft j{fe!jt!jodsfbtfe-ltp!uiblub i jhifslsftpmujpo!tymmjn bhf!dbo!cf!qsfqbsfe!!.bluijt!dbtf-ljdt zou ft jt!jogsn bujpo!jt!opulqpt jujpofe!jo!uif!eft jsfe joufsqpmujpo!qpjou!uif!qjyfmwbmmf!pduif!joufsqpmujpo!qpjouljt!joufsqpmbufe!cz!joufsqpmbujoh!nfbot/!Uif!nfuipe!tipxojo!Qht/!2!up!4!dbo!cf!vtfe!bt!uif!joufsqpmbujoh!nfbot/

\1316^ Gh/!47!it !b!@x di balt i px joh!b!t f w ou !f n cpejn f oupdu f !qs t f oujow oupo/

\1317^ _b!u f!t f wf ou !f n cpejn f ou!pom!u f !qspdf t t joh!jo!u f !psu phpobrhsbot gosn !dpf gbdjf ougosn joh!vojul2217!pg u f !t jyu !f n cpejn f ouljt !ejgf sf ou!boe!u f !pu f slvojut !bsf !dpn n po/

\1318^ _b!Gh/!47-!T3212-!T3313!t i px !u f !jojubrji{ bujpo!pgwbsjbcrfnt -!boe!wbsjbcrfn!]!pgwf sujdbrtejsf dujpo!boe!wbsjbcrfn!k pgi psj{ poubrtejsf dujpo!bsf !jojubrji{ f e!up!qspwjef !#1#

\1319^ Tvctfrvfouze!uif!gompaxjoh!pqfsbujpo!jt!qfsgpsnfe!jo!T3214/

$$G_{C}(y^{k} > 2.y^{*})2.z(*G_{C}(y^{k}, y($$

•)2.z(*•G_D\j^\k',)2.y(*•z(•G_E\j^\k', y(•z(•G_F\j^\k')

\131: ^ Tvctfrvfoumz!jo!T3215-!uif!gommax joh!pqfsbyjpo!jt!qfsgosnfe/

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\1321^ I f sf - b\j\K\c\j\K\lbsf !dpf g\dijf out -!x i jdi !bsf !qsf t f ucz!x f jhi ujoh!ef qf oef oulpo!j-!kbt !ui f !dpn qpof out !bgf s ui f !bsi phoobrhsbot cosn /

1 \1322^ Johifthon fin boofstbt johifthjuifn cpejn foulpg@jh/i38-l@ \j^k\joejdbufthiftpsiphpobhosbotopsn kdpfg@djfoupdif!ofx malqsfqbafe!cmpdl!L/!Npsfpwfs!y-(!z(!joejdbuft!uif!qptjupo!pguif!joufsqpmbujpo!qpjouljo!uif!thn fin boofstbtjo!uif!tjuu!fn cpejn fou

1323^ Tvctfrvfouz-lú f lwbsjbcrhlkjt ldpvou elvqljo!T3216-lboeljuljt lwehfeljo!T3217!x i f û f slpslopulû f lcrpdl li psj. {pouhdpn qpof ou lbsf ldpn qrhu e/l.tjZFT-lû f lqspdfttjohlsf wsot lup!T3214/ltjOP-lû f lwbsjbcrhljijt ldpvou elvqljo!T3218/ Lljt lwehfeljo!T3219!x i f û f slpslopulû f lcrpdl lwf sjdbrhdpn qpof ou lbsf ldpn qrhu e/l.tjZFT-lû f lqspdfttjohlsf wsot lup T3213/ltjOP-ljuljt lwehfelû bubmt75ldpn qpof ou lbsf lqspdfttfe-lû f sf cz!f oejohlû f lqspdfttjoh/

\1324^ __b!u fitfwfou ifn cpejn foulejggfsfoulgen !u fitjyu ifn cpejn foulpgGh/!38-!u filospofttjohljt lopultx judi felcz u filwbrwflpgj-!kil.b tu fbe-lu filospoftypolpgu fitvn !pgdspevdut!pgu filosposn bypolg_()^\Klpgu filon , 2*.u !gsbn filose!u filosposn bypolg_\Klpgu filon , 2*.u !gsbn filose!u filosposn bypolg_\Klpgu filosoftypolpgu filosposn bypolg_\Klpgu filosoftypolpgu filosoftypolpgu filosposn bypolg_\Klpgu filosoftypolpgu filosoftypolggu filosoftypolpgu filosoftypolpgu filosoftypolpgu filosoftyp

\1325^ b!puifskx pset-!uif!fn cpejn foulpg'Gh/!38!jodrmeft!uif!fn cpejn foulpg'Gh/!47/!b!uif!tfwfoui!fn cpejn fou

pg/Gh/!47-ljulit lqsfg sbcml.pltfuluf Mommf!pgb\j^\K!up!cf!mbshfljo!uffmpx.gsfrvfodz!bsfb!boe!up!tfuluf!wbmmf!pgc\j^\K!up cf!mbshfljo!uff!ijhi.gsfrvfodz!bsfb/

\1326^ Npsf pwf s!u f!commox joh!it!hf of sommo!f t ubcriti f e-!cvulu it!it!opulrim juf e/

TqfdjÖdb noo-!x i fo!uif!usb otgo sn !dpfgÖdjfo dpguif!ijhi.gsfrvfo dz!b sfb!jt!sfev dfe-!uif!go napxjo h!tfujo h!jt!tvgÖdjfo uoz qpttjc:ft/

Lijt !qsf gf sbcrin!up!f yqf sin f oubrazi!dbrdvrbuf !ui f !dpf gDdjf out f ujoh/

6

21

26

36

41

46

61

66

\1327^ Ui f!t zou ftjt!pgblqmsbrjuz!pgjn bhft!cz!qsf qbsjoh!ui f!psu phpobhusbot gsn !dpf gfujf ou !i bt !cf f o!ef t dsjcf e bcpwf/!Tjodf!ui f!di bsbduf sjt ydt!pgui f!t jyui!boe!t f wf ou !f n cpejn f out!jwf !jo!ui f!qspdf t t joh!pgebub!vt joh!ui f!psu ph. pobhusbot gsn -!ui f!dpot yjwypot!ps!pqf sbypot!pgpui f slqpsypot!t vdi !bt!ui f!n pypo!wf dups!pqf sbypo!vojuboe!ui f!t zo. ui ftj[joh!vojubsf!opulrjm juf e/!Ui f!n pypo!wf dups!pqf sbypo!vojui bt!cf f o!ef t dsjcf e!cbt f e!po!ui f!wf dups!dbruvrbuypo vtjoh!ui f!psui phpobhusbot gsn !qspqpt f e!cf gsf!cz!ui f!qsf t f oubqqrjulbou!cvului jt!jt!opulrjm juf e/!Dpowf oypobrhm f ui pet t vdi !bt!b!n f ui pe!pgef uf dyoh!b!qpt jypo!jo!x i jdi !ui f!t r vbsf!t vn !pgejgf sf odf t !pgqjyf rh!po!ui f!sf brihqbdf!jt!n jojn vn n bz!cf!vtfe/

\1328^ Npsipwis-ljolu flebublqspdfttjoh-lbtltipxolczlu flgompxjohlfrvbujpo-lbtljn qm/lpqfsbujpoln bzlcflqfsgpsn fepolu flpsu phpobhosbotgpsn ldpfgfbljfoutlpgu flopu elempdl lBlpgu fln.u lgsbn flboelu flempdl lC(i bwjohlbtn bm/intufsspspgu fl)n, 2*.u lgsbn f/

\1329^ TqfdjÖdbmoz-luif!bcpwf.eftdsjcfe!frvbujpot!pguif!ebub!qspdfttjoh!dbo!hfofsbmoz!sftvmdjo!uif!gompoxjoh/

$$F_{k}[i][j] = \sum_{q=1}^{p} \alpha_{q}[i][j] \cdot F_{q}[i][j] + \beta[i][j] \cdot F_{k}[i][j]$$

... (21)

\132:^ __bluif bocpwflfrvb ujpo-lr lef op uftlompoll lovn of stop sn felpoluifl)n, 2*.uilgsb n f-lqlef op uftluiflovn of stpgcmpoll t vtfeljoluifleb ub lqsp offttjohlpoluifl)n, 2*.uilgsb n f-lboe b_r lef op uftlb ldpfg Dujfoluiflompoll iovn of str/lub luiflyb n qm pg Gh/l47-ltjo offlgovsk ompoll tlpg uifl)n, 2*.uilgsb n flb sflvtfe-lq!>!5/

\1331^ Tqf djÖdbmæ-ljo!u f lpqf sbujpo!pgu f lt vn lpgqspevdut lpgu f lusbot gosn ldpf gÖdjf oulG_ij^Nk'jo!u f lpsu phpobhusbot .
gosn ldpn qpof oulj-lklpgu f lopuf elcmpdl !B!pgu f !n .u lgsbn f -lboe!u f lusbot gosn ldpf gÖdjf oulG_ij^Nk'jo!t pn f !cmpdl t !Gof df tt bsz!goslu f lebub!qspdf tt joh!pgu f !)n , 2*.u lgsbn f -!u f !psu phpobhusbot gosn ldpf gÖdjf oulG_ij^Nk'!pgu f !of x !cmpdl
L!jt !dbmdvmbuf e/

\\1332^ Npsf pwf s!bt !t i px o!jo!G|ht /!38-!47-!x i f o!u f !wbmf !pgG_\j^\K!ef qf oet !po!u f !wbmf !pgy(-!z(!joejdbujwf !pgu f ejt ubodf !pgu f !jouf saprhujpo!qpjou!u f !wbmf !dbo!cf !sf qsf t f ouf e!cz!u f !gpmpx joh/

$$F_{k}[i][j] = \sum_{q=1}^{p} h(x', y') \cdot \alpha_{q}[i][j] \cdot F_{q}[i][j] + \beta[i][j] \cdot F_{k}[i][j]$$

... (22)

\1333^ I f sf -i)y(-!z("lef opuf t !bo ijouf sqprhujoh !pqf sbujpo !godujpo !ef qf oef oulpo !u f !ejt ubodf !cf ux f f o !u f ijouf sqprhujpo qpjouboe!bo!pct f swbujpo!qpjouf!Qpstu f !godujpo-!rjof bsijouf sqprhujpo-!dvcjd!dpowprnujpo!jouf sqprhujpo-!boe!u f !rjof !dbo cf !dpot jef sf e/!Ui f !psu phpobrhusbot gpsn !dpf gDijf oulpgu f !of x !crpdl !dbo!cf !qsf qbsf e!x ju !i jhi !gsf f epn !ef hsf f !gspn ui f !crpdl !jogpsn bujpo!pgb!qrnsbrjruz!pggsbn f t !vt joh!ui f !f r vbujpot!)32*!boe!)33*/

\1334^ Npsf pwfsljolu f !tjyu !boe!tf wf ou !f n cpejn f out-!u f !eft dsjqujpo!i bt !cff o!cbt f e!po!EDU!pgu f !cmpdl !pg9

×!9!qjyf m!jo!u f !psu phpobmusbot gosn -!cvuljuhpft !x ju pvult bzjoh!u buu f !ovn cf slpgqjyf m!jt !opuljm juf e!up!u jt /

\1335^ Gvsu f sn psf-ljolu f !tjyu !boe!t f wf ou !f n cpejn f out-!u f !dpoujovpvt !jn bhft !pgu f !n .u !gsbn f !boe!u f !)n , 2*.

u !gsbn f !i bwf !cff o!eft dsjcfe-!cvuldpoujovpvt !pslejt dpoujovpvt !jn bhft !bsf !opuljm juf e/!Ui f !n pujpo!wf dups!boe!u f
psu phpobmusbot gosn !dpf godjf oucf ux f f o!u f !n .u !gsbn f !boe!u f !)n , o*.u !gsbn f !)o μ!2*!dbo!obuvsbmus!cf !t zou f t j{f e
vt joh!u f !bcpwf !uf di ojr vf /

\1336^ Bt left dsicfelbcpwf-lbddpsejohluplui f lqsft fouljowf ouppo-bx i folui f lpsui phpobhosbot gosn ldpf gbdif oupgui f lof x cmdl ljt lqsf qbsfelcbt felpolui f lpsui phpobhosbot gosn ljogosn bujpolpdblqmsbrjoozleggbn ft-lboelui f ljowfst f lpsui phpobhosbot gosn ljogosn bujpoljt lqpt jujpof elef wjbujohlgspn lui f lt bn qrfnlqpjoulpdpsjhjobrljogosn bujpo-lblqmsbrjoozlegjn bhft ldbolcft zoui ft if felx jui pvulbozlejt psef s'

\1337^ Bo!fjhi ui!f n cpejn foulpguif!qsftfouljowfoujpo!xjmmofyulcf!eftdsjcfe/!Gjh/!48ljt!blcmpdl!ejbhsbn!tipxjohluifdpotyjwypo!pguif!jn bhf!qspdfttjoh!bqqbsbuvt!bddpsejohlup!uif!fniui!fn cpejn foulpguif!qsftfouljowfoujpo-luif!dpo.
tyjwyjoh!fminfout!tjnjmbs!up!uiptf!pgGjht/!25!boe!36!bsf!efopufe!cz!uif!tbnf!sfgsfodf!ovnfsbm-!boe!uif!eftdsjqypouifsfpgjt!pnjufe/

\1338^__\b!Gh/!48-lb!t f rhdypolvoju243!\text{wehf t !b!yin f !jn bhf !\p!cf !t f ubt !b!sf gf sf odf !\text{gspn f !\text{gspn ijn bhf !\potspn b\text{ypolpolpo}}}})o, 2*!\text{gspn f t !t \text{ \text{wsf e !\pi} in f !t \text{ \text{wsh f !voju212/!...ljt !opx !bt t \text{ \text{vn f e !\text{u} bu \text{u} f !\text{sf of sf odf !\text{gspn f !t f ubddpsejoh!\text{\text{when f ou sf t \text{vnijt !\text{u} ob.\text{y\text{m} ra!t f u\text{\text{up !\text{gspn f !H/!B!\text{gspn f !dpousprhvoju244!\text{!t !n f bot !\text{\text{yst f rhd\text{y}oh!\text{\text{v} p !\text{u} f !\text{y} bhf t !\text{b! f !\text{y} bn f !\text{hose!\text{u} f !\text{y} in bhf t !\text{pof !\text{gspn f !\text{hose} in f !\text{y} in bhf !\text{ypf poh f !\text{\text{y} bn f !\text{\text{w} f !\text{ \text{u} f !\text{y} in bhf !\text{\text{y} in bhf !\text{\text{y} in f !\text{\text{w} f !\text{\text{gspn f !\text{\text{W} in f !\text{\text{w} f !\text{\text{y} in bhf !\text{\text{y} in bhf !\text{\text{y} in bhf !\text{\text{w} f !\text{\text{y} in bhf !\text{\text{w} in bhf !\text{\text{y} in bhf !\text{y} in bhf !\text{\text{y} in bhf !\text{y} in bhf !\text{\text{y} in bhf !\text{y} in bhf !\text{y} in bhf !\text{y} in bhf !\text{y}

\1339^ Ui f!n pypolwf dupslpqf sbypolvojul226!n f bt vsf t!n pwf n f oubn pvoupgqbsjbrin pwf n f oubt!ui f!n pypolwf dups cbt f elpolui f!ejgf sf odf!pglw p!wqf t!pgjn bhf t!pglu f!gsbn f t!H!boe!! /!Ui f!dpot ywypo!pglui f!n pypolwf dupslpqf sbypovojul226!jut frigit!ui f!t bn f!bt!ui-bulpglui f!gpvsui!up!t f wf oui!f n cpejn f out/

\1342^ Gh/l4: !tipxt!uf!fybn qmlpgb!hfofsbmlwbqmbdjbo!fehf!fyusbdypo!Omufs'
\1343^ Opx-!bttvnjoh!ubuuf!qjyfmlwbm/f!jo!dppsejobuf!)y-!z*!po!uf!jnbhf!pg)n,t*.uigsbnf!)1 • !t • !4*!jt!tfdup!g
)y-!z*-boe!uflwbm/f!bg/fskuf!fehf!fyusbdypo!qspdfttjoh|jt!tfdup!!t)y-!z*-luf!gompxjoh!pqfsbypo!pduf!tvn!pgqspevdut
jt!qfsgpsnfe!jo!uf!fehf!fyusbdypo!OmufspdGh/!4:/

$$I_{1}$$
)y- z* > q)y.2- z.2*, q)y- z.2*, q)y, 2- z.
2*, q)y.2- z*.9q)y- z*, q)y, 2- z*, q)y.2- z, 2*, q)y-
z, 2*, g)y, 2- z, 2*

\1344^ _b!Gjh/!49-!fehf!tusfohui!fwbnnbujpo!vojut!316-!317-!318-!319!bsf!nfbot!gosljoufhsbujoh!fehf!tusfohuit!fy.usbdufe!cz!uif!fehf!tusfohuit!fy.usbdufe!cz!uif!fehf!tusfohuip!312!up!315!pwfsuif!foujsf!jnbhf/!Xifoluif!ovncfslpgwfsujdbnnujyfnhlpguif!foujsfjnbhf!jt!tfulup!Vboe!uif!ovncfslpguipsj{poubnajyfnhljt!tfulup!!-!uif!fehf!tusfohui!Qt!pguif!)n,t*.uigsbnfjt!dbndwnbufebt!gompuxt;

$$P_{s} = \sum_{x=0}^{H} \sum_{y=0}^{v} k_{s}^{i}(x, y) \qquad ... (24)$$

jo!x i jdi

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66

I (,)y-!z*!>!}I,)y-!z*}-!x i f o!}I,)y-!z*} µ!u !)u !ef opuf t !b!qsf t f du sf t i pre!wbrxf *-!boe

16)y-!z*!>!1!jo!u f!dbtft!pu f slu bo!u f!bcpwf/

\1345^ B!n byjn vn !f ehf !t us ohu !ef uf sn jobupolvoju31: !ef uf sn jof t !b!gsbn f !t !jotx i jdi !Qt !pcubjof e!cz!f bdi !pgu f f ehf !t us ohu !f wbmbupolvojut!316!up!319!jt !n byjn vn !bt !u f !sf gf sf odf !gsbn f /!Tqf djÖdbnæ!u f !f ehf !t us ohu !x i jdi jt !b!vojr vf !f wbmbupolgvodupo!jt !t f ulboe!u f !gsbn f !jotx i jdi !u f !f ehf !t us ohu !jt !f wbmbuf e!bt !cf joh!nbshf t ulpwf slu f ouisf !jn bhf !jt !t f rhduf e!bn poh!u f !t upsf e!qmsbrjnæ!pggsbn f t !pgjn bhf t/

\1346^ Up!t fului f!jn bhf!x jui !ui f!rbshft uf ehf!t usf ohui!bt!ui f!sfgfsf odf!gsbn f!jt!bewboubhf pvt!opuporalx i fo!ui f n pujpo!widupsjt!tlbrodvrbuf e!bt!eft dsjcfe!houf slcvulbrhpkx i fo!ui f!ebublqspdfttjohlpgui f!pui fspckidugsbn ft ijt!tqfspsn fe/ ub!ui f!fwbmbujpo!cz!ui f!fehf!t usfohui-!bo!jn bhf!x i ptf!gpdvt!jt!n pt uddribsna!qjdl fe.vq!dbo!cf!bttvn fe!bn poh!ui ft upsfe!qmsbrjoze!pggsbn ft/!Ui fsfgpsf-!ui f!jn bhft!pgui f!pckidugsbn ft!pui fslui bo!ui f!sfgfsfodf!gsbn f!tfswf!up!bubdi bo!beejujpobrhwbmf!up!ui f!jn bhf!rvbrjoze!pgui f!sfgfsfodf!gsbn f-!boe!ui f!foi bodfn foupgui f!jn bhf!rvbrjoze!frvbrhp!pshsfbufslui bo!ui bulpgui f!sfgfsfodf!gsbn f!tjohra!dbo!cf!fot vsfe!fwfo!buh.jojn vn /

\1347^ Npsfpwfs!gpstuif!dpot ujuvujpo!pdGjh/!49-!up!gbdjrjabtf!uif!eftdsjqujpo-!uif!fybn qrfn!jo!xijdi!bintgsbnft!bsfqspdfttfeljo!b!spx!ibt!cffoleftdsjcfe-!cvduif!dpot ujuvujpo!nbz!obuvsbnaa!dpnqsjtf!b!tjohrfn!fehf!fyusbdujpo!vojuboefehf!tusfohui!fwbrwbujpo!vojulgpstb!wfsujdbrtqspdfttjoh/

 $\label{thm:continuous} $$1348^ Nps^p_s!jo!u^f!frvbujpo!)35^!u^f!bctpmu^f!wbmf!pgl_t)y-!z^!jt!vtfe!goslu^f!dbmdvmbujpo!pgl_t(y-!z^-!cvuu^ftrvbs^!pgl_t)y-!z^!n^f. bz!obuvsbmoolcf!vtfe!up!qfsgosn_!u^f!pqfsbujpo/$

\1349^ Ui f!ebub!qspdfttjoh!voju247!xjmlofyulcf!eftdsjcfelxjui!sfgfsfodf!\p!Qh/!51/

\134: ^ _b!Gh/!51-lb!dppsejobuf!n bobhf n f ouvojul86: !n bobhf t !u f !qpt jujpo!pg u f !gsbn f !H!bt !u f !sf gf sf odf !gsbn f up!x i jdi !u f !crpdl !pg u f !gsbn f !l !bt !u f !pclf dugsbn f !jt !up!dpssf t qpoe!jo!bddpsebodf !x jui !u f !wf dupsldbrownbuf e!gspn u f !n pujpo!wf dupslpqf sbujpo!vojul226/!Ui f !dppsejobuf !n bobhf n f ouvojul86: !pvuqvut !bo!beesf t t !jo!x i jdi !u f !f wbrnbujpo gvodujpo!pg u f !f r vbujpo!)8*!jt !n jojn v n /

\1351^ Bo!O ×!O(lcmpdl !gosn johlvojul869!gosn t !u f !jn bhf !pdu f !gon f !l !joup!b!cmpdl !jo!u f !vojulpgO ×!O!qjyf m'!Ui jt n f bot lepf t lopulof f eluplof lqf sgosn f e ijo!u f lebublqspdf t t johlvojul247-jigu f lqjyf mubmrf ijogosn bypolpgiu f lcmpdl !)sf g ssf e up!bt !u f !opuf e!cmpdl *!vt f e!jo!u f !qsf wjpvt .t ubhf !n pujpo!wf dups!pqf sbypo!vojul226!jt !sf ubjof e/

\$\lambda 1352^ Tjn jrbsxx-lbo!O \times!Olcrpdl !gsn joh!voju864!gsn t !u f !crpdl !pdu f !O \times!Olqjyf rhvojupgu f !gsn f !H!cbt f e!po u f !beest t t !sf df jwf e!gsn !u f !dppsejobu !n bobhf n f ouvoju86: /!Ui jt !n f bot !epf t !opulof f e!up!cf !qf sgsn f e!jo!u f ebub!qspdf t t joh!voju247-!jdu f !qjyf rhwbrwf !jogsn bujpo!pdu f !crpdl !)sf g sef e!up!bt !u f !f seps!n jojn vn !crpdl *!x i pt f f wbrwbujpo!gvodujpo!jt !n jojn vn !boe!u f !crpdl !qpt jujpof e!jo!u f !qf sjqi f se!pgu f !f seps!n jojn vn !crpdl !)sf g sef e!up!bt u f !qf sjqi f sbrtcrpdl *!bsf !sf ubjof e!bn poh!u f !crpdl t !qsf qbsf e!boe!f wbrwbuf e!jot jef !u f !qsf wjpvt .t ubhf !n pujpo!wf dups pqf sbujpo!voju226/

\1353^ Opx-!uif!opufe!cmpdl!po!uif!gsbnf!l !jt!tfulup!uif!cmpdl!B-!boe!uif!ssps!njojnvn!cmpdl!xjui!sftqfulup!uifcmpdl!B!po!uif!gsbnf!H!jt!tfulup!uif!cmpdl!C(!N psfpwfs!bnpoh!uxp!uzqft!pgcmpdlt!gpsnfe!cz!ipsj{poubrtijgjoh!fbdicz!poflqjyfrkap!uif!mpdlboe!uif!sjhiutvtjoh!uif!cmpdl!C(!bt!uif!sfgsiodf-!uif!cmpdl!xiptf!fwbmobujpo!yodujpo!jt!fwbmwbufebt!cfjoh!tnbmmjt!tfulup!uif!cmpdl!D!!Tjnjmbsmz!bnpoh!uxp!uzqft!pgcmpdlt!gpsnfe!cz!tijgjoh!fbdi!cz!pof!qjyfrkvqxbseboe!epxoxbse!jo!uif!wfsijdbrhejsfdujpo!vtjoh!uif!cmpdl!C(!bt!uif!sfgsiodf-!uif!cmpdl!xiptf!fwbmwbujpo!gvodujpo!jtfwbmwbufe!bt!cfjoh!tnbmmjt!tfulup!uif!cmpdl!E/

\1354^ Npsf pwf s!u f !cmdl !x i jdi !i bt !y!dppsejobuf !pgpsjhjo!pgu f !cmdl !D!boe!z!dppsejobuf !pgpsjhjo!pgu f !cmdl !E jt !t f ulp!u f !cmdl !F.!Ui f !cmdl !F!ef wjbuf t !gspn !u f !cmdl !C(!cz!pof !qjyf rfjo!f bdi !pgu f !i psj{ poubriboe!wf sijdbrisejsf dujpot / \1355^ Bo!bwf sbhf !wbrwf !dbrdvrhujpo!voju865!jt !n f bot !gssldbrdvrhujoh!u f !bwf sbhf !wbrwf !pgqjyf rhwbrwf t !x ju jo!u f cmdl !B!bt !u f !opuf e!cmpdl /!X i f o!u f !psjhjo!dppsejobuf !pgu f !cmpdl !B!jt !t f ulp!)b1-!c1*-!u f !bwf sbhf !wbrwf !Ug!pgu f cmpdl !B!jt !dbrdvrhuf e!bt !gmpx t /

$$T_{A}=1/N^{2}\times\sum_{x=a_{0}}^{a_{0}+N-1}\sum_{y=b_{0}}^{b_{0}+N-1}f_{H}(x,y) \qquad ... (25)$$

61)jolx i jdi lg)y-lz*lef opuf t lui f lqjyf rhwbrwf !pgdppsejobuf !)y-lz*!pgui f !gsbn f !l *

56

66

\1356^ Bo!bwf sbhf !wbmf!tfqbsbijpo!voju866!jt!n f bot!gpsltfqbsbijoh!u f!dbmdvmbufe!bwf sbhf !wbmf!U_B!gppn !f bdi qjyf mjo!u f!cmpdl!B!cz!t vcusbdijpo/!X i f o!u f!wbmf!bgf slu f!t vcusbdijpo!jt!tfulup!h_|)y-!z*-!dbmdvmbujpo!jt!qf sgpsn f e!jo u f!gpmpx joh!frvbijpo!)37*/

$$h_1$$
)y- $z^* > q$)y- $z^*.U_B$)37*

qpjodjt !u f !psjhjo!pgu f !crpd! !B-!boe!jt !bo!bssbohf n f odqpjod

\1363^ Ui.f!frvbijpo!)42*!n f bot !ui bdu f!bwf sbhf!wbrwf!pgu f!crpdl!B!jt!tvct ijuv fe!gslu f!bwf sbhf!wbrwf!pgu f crpdl t!C(-!D-!E-!F/!Beejijpobrælu f!bwf sbhf!wbrwf!up!cf!tvct ijuv fe!jt!ef qf oef odpo!ui f!jouf saprbujpo!qpjodpgu f!crpdl B-!boe!ui f!jrof bs!pqf sbijpo!pgu f!bwf sbhf!wbrwft!pggvslcrpdl t!jt!qf sgpsn fe/!b!pu fsx pset-!ui f!ED!dpn qpof odpgu f crpdl!B!jt!di bohfe!tp!bt!up!cf!Ödgpslui f!crpdl|t!C(-!D-!E-!F!po!ui f!sfg sf odf!gsbn f-!tp!ui bdporz!ui f!BD!dpn qpof odpg ui f!crpdl!B!jt!vijriffe/

 $\label{thm:continuous} $$1364^-$ Uif!ebub!qspdfttjoh!voju247!ibt!cffoleftdsjcfe!bcpwf-!cvduif!fjhiui!fncpejnfoujt!opulmijtfe!\p!uifbcpwf.eftdsjcfe!fybnqrfv!Tjodf!uif!crpdlt!C(-!D-!E-!F!rbshfrzd!pwfsrbq!pof!bopuifs!uifsf!nbz!cf!op!rbshf!ejggfsfodfbnpoh!uif!dbrdvrbuife!bwfsbhf!wbrwft/!Jo!uijt!dbtf-!b!tjnqrfn!nfuipe!nbz!cf!vtfe!xiijdi!dpnqsjtft!beejoh!porzluifbwfsbhf!wbrwf!Uc(!pgluif!crpdl!C(!p!hl)y-!z*/$

\1365^ Gh/!53it i px t !u f !Qbx di bsulpgu f !pqf sbujpo!qspdf ev s !pgs qf buf e!qspdf t t joh!jodrwejoh!u f !qspdf t t joh!gos dbrotvhoujoh!boe!bssbohjoh!u f !n pujpo!wf dups!df ou sjoh!po!u f !gsbn f !dpousprtvoju!244!qbsujdvrbszz!x i f o!u s f !ps!n ps gsbn f t !bs !vt f e/

\1366^ Gistuljo!T: 12-!uif!fehf!tusfohui!jt!fwbm/bufe!gos/fbdi!pg)o, 2*!gsbnft!gspn!uif!n.ui!gsbnf!up!uif!)n, o*.ui gsbnf/!Tvctfrvfouze!jo!T: 13-!uif!gsbnft!bsf!dpnqbsfe!xjui!fbdi!puifs/

\1367^ Tvctfrvfouze-ljo!T: 14-luif!)n, q*.ui!gebnf!ib wjohluif!n byjn vn!fehf!t usfohui!jt!tfubt!uif!gebnf!H-lxijdijt!uif!sfgfsfodf!gebnf/!Ofyuljo!T: 15-!wbsjbcrfnt!t!boe!r!bsf!jojubrjntfelup!qspwjef!1/!JJjt!uifo!kvehfe!jo!T: 16!xifuifspslopuluif!wbsjbcrfnt!jt!frvbrhup!q/!Uijt!efufsnjoft!xifuifslpslopuluif!gebnf!up!cf!qsftfouze!qspdfttfeljt!uif!sfgfsfodfgebnf/

\1368^ _Uju f !gsbn f !t !up!cf !opx !qspdf t t f e!jt !opdu f !sf g sf odf !gsbn f -!ju]t !kvehf e!jo!T: 17!x i f u f slpslopdu !f r v brh {f sp/!Ui jt !ef uf sn jof t !x i f u f slpslopdu f !sf qf bujoh!gsf r v f odz!pg u f !qsf t f odqspdf t t joh!jt !Öst dujn f /!Ujr !f r v brh!{f sp-u i f !gsbn f !H!jt !bssbohf e!jo!T: 18-!boe!u f !wbsjbcrh!r !jt !dpvou e!vq!jo!T: 19/!Ub!u f !of hbujwf !ef uf sn jobujpo!pgT: 17-!ju]t ef uf sn jof e!u bulu f !qspdf t t joh!jt !sf qf buf e!ux jdf !psln psf -!boe!u f !gsbn f !H!bt !u f !sf g sf odf !gsbn f !jt !brsf bez!bssbohf e-t p!u bulT: 18-!T: 19!bsf !kvn qf e/

\1369^ Tvctfrvfouzeljo!T: 1: -!uif!n pujpo!wfdupsljt!dbrodvrbufe!cfuxffo!uif!gebnf!H!boe!uif!)n, t*.uigebnf!)gebnf! + 1 */!Ofyu!bgfsluif!ebub!qspdfttjoh!pguif!gebnf!! | ijo!T: 21-!uif!bsebohfnfoupguif!gebnf!! | ijt!qfscpsnfe!jo!T: 22/!Bgfs dpvoujoh!vq!uif!wbsjbcrhit!jo!T: 23-!juljt!|wehfe!jo!T: 24|xifuifslpslopuuif!sfqfbujoh!gsfrvfouz!sfbdift!o.uinft/!Jopu-juljt!|wehfe!uibulopo.qspdfttfe!gebnf!jt!tupsfe-!uif!qspdfttjoh!sfwsot!up!T: 16-!boe!uif!tjnjrbs!qspdfttjoh!jt!sfqfbufepo!uif!puifslgebnft/

41 \136:^ Xifoluif!b ssbohfn foulp gb mbuif!tup sfelgsbn ftljtldpn qmfufe-lp oflgsbn flpgjn b hfljogo sn bujpoljtltzouiftj{feuifsfczlfoejohluif!qsp dfttjoh/

\1371^ Bltf sft !pgqspdf tt joht !pgu f !f jhi u !f n cpejn f oui bwf !cf f o!ef t dsjcf e-!boe!u f !n pt udi bsbdu sjt ujd!qbsupg u f !f jhi u !f n cpejn f ouijit !jo!u f !t f rhdujpo!voju243/!Ui f sf gpsf -lu f !dpou out !pgu f !n pujpo!wf dups!pqf sbujpo!voju226-u f !ebub!qspdf t t joh!voju247-lu f !bssbohf n f oulqspdf t t joh!voju216-!boe!u f !rjih f !bsf !opurijim juf e/!Ui f !n pujpo!wf dups pqf sbujpo!dbo!cf !sf brjkf e!f wf o!jo!u f !n f u pe!opuvt joh!u f !psu phpobrusbot gpsn -!boe!u f !dpot ujuvujpo!n bz!dpn qsjt f porz!bssbohjoh!u f !qjyf rhwbrwf !pgf bdi !pclf dugsbn f !x ju pvulqspdf t t joh!boz!ebub!pgu f !pclf dugsbn f /

\1372^ Npsfpwfshiffwbmbypobyodypobybiffehftlusfohu bybiffrvbypol)35* it bouhim jufe/Uifbympux johfrvbypo)43*!dbolbmplcfldpotjefsfelbtluifln pejÖdbypolpguiflfrvbypol)8*;

$$P_{s} = \sum_{x=0}^{H} \sum_{y=0}^{v} k_{s}^{!}(x,y) \qquad ... (32)$$

jo!x i jdi

51

56

I (,)y-!z*!>!1!jo!u f !dbt f t !pu f slu bo!u f !bcpwf/

\1373^ Uijt!n f bot!u bulu f!ovn cfslpgqjyfmljt!dpvoufe!x i fo!u f!wbmf!bgfslu f!fehf!fyusbdujpo!Ömfslsfbdift!b dfsbjo!u sfti pme!wbmf!psln psf/!Fwfo!jo!u f!frvbujpo!)43*!u f!fehf!tusfohu !pgu f!foujsf!jn bhf!dbo!tvgÖdjfouze!cf hsbtqfe/

\1374^ Npsf pwf słu f ldpf godjf odpgu f lf ehf lf yusodujpoloni sljt lopdrjm juf eluplu f ldpf godjf odt i px oljolojh/l4: -lboelu f Oni sli bwjohlblt uspohf slopjt f lsf t jt ubodf ln bzlcf lvt f e/

\\1375^ Gvsifsn psf-lgoslif!fwbmbujpo!pglif!fehf!tusfohui-ltztufntljo!xijdi!op!fehf!fyusbdujpo!Qwfsljt!vtfe!tvdibt!b!tztufn!pgqfsgpsnjoh!efufsnjobujpo!cbtfe!po!uif!usbotgpsn!dpfgQdjfoupglif!ijhi.gsfrvfodz!dpnqpofoupglifpsiphpobrhusbotgpsn!nbz!brhup!cf!dpotjefsfe!!.b!uijt!dbtf-!uif!gsbnf!jo!xijdi!uif!ijhi.gsfrvfodz!qpxfsljt!rbshf!jtfwbmbufe-!boe!uif!gsbnf!xiptflgshff!xiptflgshff!ttfdbt!uif!sfgsfodf!gsbnf/

\1376^ Beejypobraz jolu f !f jhi u !f n cpejn f ou!u f !f ehf !jogpsn bypo!jt !vt f e!jo!u f !jn bhf !di bsbdu şt yd!bn pvou!cvu

- u jt ljt lopuljim juf e-lboelu f lpu f sijn bhf ldi bsbduf sjt ujdlbn pvoun bzlcf lvt f eluplqf sgpsn lu f lf wbmbypo/
- \1377^ Gh/!54ljt !b!Qpx di bsult i px joh!u f !pqf sbujpo!qspdf evsf !bddpsejoh!up!b!ojou !f n cpejn f oulpgu f !qsf t f ouljowf o.
 ujpo/!.b!u f !ojou !f n cpejn f ou!ponz!u f !t f rhdujoh!n f u pe!cz!u f !t f rhdujpo!voju243!pgGh/!48!jt !ejgf sf ou!boe!u f !pu f s
 vojut !bsf !u f !t bn f /
- 1378^ Npsfpwfsłjo!uif!Q5x dibsupg/Qh/!54!uifsf!jt!tipxo!bo!fybn qmfljo!xijdi!pof!gsbnf!pgijhi.sftpmujpo!tujmm jn bhf!jt!qsfqbsfelcbtfe!po!uif!jn bhf!jogosn bujpo!pg)o, 2*lgsbnft!gspn!uif!n.ui!gsbnf!up!uif!)n, o*.ui!gsbnf/
- \1379^ __b!blejwjtjpo!qspdftt!pgT2112-!uif!joufhfs!qpsujpo!pguif!ejwjtjpo!pgwbrwnf!o!cz!3!jt!tvctujwufe!bt!q/!Uif!bduvbm qspdfttjoh!dbo!cf!sfbrjwjfe!cz!cjutijgjoh/!Tvctfrvfouzo!jo!T2113-!uif!)n,q*.ui!gsbnf!jt!tfubt!uif!gsbnf!H!xijdi!jt uif!sfgfsfodf!gsbnf/!Ofyuljo!T2114-!wbsjbcr/nt!t!boe!r!bsf!jojujbrjwjfe!up!qspwjef!1/!Uijt!uifo!wehfe!jo!T2115!xifuifs psłopuluif!wbsjbcr/ni!t!jt!frvbr/mp!q/!Uijt!efufsnjoft!xifuifs!psłopuluif!gsbnf!up!cf!qsftfouzo!qspdfttfe!jt!uif!sfgfsfodf gsbnf/

 - \1381^ Tvctfrvfouze-ljo!T2119-lû f!n pûpo!wfdupsjt!dbrodvrboufe!cfuxffo!û f!gsbn f!H!boe!û f!)n, t*.û !gsbn f!)gsbn f I*/!Bgfslû f!ebub!qspdfttjoh!pgû f!gsbn f!I !jo!T211:-lû f!bssbohfn foulpgû f!gsbn f!I !jt!qfsgpsn fe!jo!T2121/!Bgfs dpvoyoh!vq!û f!wbsjbcrh!t!jo!T2122-ljûjt!wehfe!x i fû fslpslopulû f!sfqfbyoh!gsfrvfodz!sfbdift!o.ýn ft/!X i fo!opo. qspdfttfe!gsbn fijt!t upsfe-lû f!qspdfttjoh!sfwsot!up!T2115-lboe!û f!tjn jrbs!qspdfttjoh!jt!sfqfbufe!po!û f!pû fs!gsbn ft/\1382^ X i fo!û f!bssbohfn foulpgbrobû f!t upsfe!gsbn ft!jt!dpn qrhufe-!b!tjohrh!jn bhf!jt!tzoù ftj{fe-!û fsfcz!foejoh û f!qspdfttjoh/
 - \1383^ Bt!eftdsjcfe!bcpwf-!uif!ojoui!fncpejnfoujt!dibsbdufsj{fe!jo!uibuluif!tfmbdupo!pguif!sfgfsfodf!gsbnf!jtefufsnjofe!bddpsejoh!up!uif!joqvuufe!gsbnf!psefsf
- 36 \1384^ G|h/l55!tipxt!uif!efufsnjob ijpo!pguif!sfgfsfodf!gsbnf!xifo!Öwf!gsbnft!bsf!tupsfe/!Uif!gsbnf!tipxolcz tmboujoh!mjoft!jt!uif!sfgfsfodf!gsbnf/
 - \1385^ Xifo!Owf!gebrnft!pgjnbhft!bef!tupefe-!o!>!5-!uifo!uif!ejwjtjpo!cz!3!eftvmut!jo!q!>!3-!tp!uib duif!)n, 3*.ui
 joufenfejbuf!gebrnfljt!tfulbt!uif!efgfefodflgebrnf/!Uif!efgfefodflgebrnfljt!dpnqbefelx.jui!uif!puifekgovs!gebrnft!up!qfegpen
 uif!qepdfttjoh/
- \1386^ Juif!ovn cf slpgt upsf elgebn ft!jt!bo!f wf olovn cf sluif!ejwjt jpo!pgo!cz!3!sf t vmt!jo!blopo.jouf hf s!Uif sf gpsf-uif!gbn f!dboopuf ybdumz!cf!jouf sn f ejbuf-lcvuluif!gbn f!cf gpsf!boe!bgf sluif!n jeerfn!n bz!cf!tf lbt!uif!sf gf sf odf!gbn f)jo!uif!Qbx di bsulpgQjh/!54-luif!gbn f!jt!cf gpsf!uif!n jeerfn*/!Tqf djQblomze!jo!uif!n f uipe!bddpsejoh!up!uif!fn cpejn f ou pgluif!Qbx di bsulpgQjh/!53-luif!tf rfndujpo!pgluif!sf gf sf odf!gbn f!jt!tf ulcbt f e!po!#uif!jn bhf!di bsbduf sjt ujd#!Uif!fehf t usf ohui!jt!f wbmbuf e!bt!uif!f wbmbujpo!gvodujpo!xijdi!dbo!sf qsf tf ouluif!di bsbduf sjt ujd!bn pvoulpguif!n bhf!n pt u sf n bsl bcmz!Jujt!df subjo!uibuxif olt frindujpo!jt!qf sgpsn f e!cz!uif!jn bhf!di bsbduf sjt ujd-luif!jn bhf!i bwjoh!bo!pquin vn jn bhf!r vbrjnuz!dbo!cf!tf ubt!uif!sf gf sf odf!gsbn f/
 - \1387^ I px f wf sit jodf !u f !dpoujovpvt !jn bhft !bsf !i boerfie-!u f !jn bhf !dboopulof df tt bsjzz!cf !t bje!up!cf !pqujn vn !jo qpjoulpgujn f /!Ui f sf gpsf -!jo!u f !f n cpejn f oulpgu f !Qbx di bsulpg@jh/!54-!tf rfidujpo!jt !qf sgpsn f e!cz!n bl joh!n vdi !pg#u f ujn f !dpssf rbujpo!pgu f !jn bhft #!X i f o!u f !jouf sn f ejbuf !jn bhf !jo!u f !yn f !byjt !jt !vt f e-!boe!dpn qbsf e!x ju !u f !gsbn f t pgu f !t upsf e!jn bhft -!boe!u f !jn bhf !dpoujovjuz!jt !dpot jef sf e-!u f !df ousbrhjn bhf !i bwjoh!u f !i jhi f t ujn bhf !dpssf rbujpo dbo!cf !f t ujn buf e/!Tqf dj@dbroo!t jodf !u f !ujn f !ef wjbujpo!jt !n jojn vn -!u f !ejogf sf odf !cf ux f f o!f bdi !gsbn f !boe!u f !sf g s f odf !jn bhf !dbo!cf !n jojn j{f e/
 - \1388^ Uif If n cpejn fout lpguif lgaft fouljowf oujpoli bwf !cffoleft dajcfe!bcpwf-!cvulb!dpn qspn jt f !cf ux f foluif !Cpx. dibat!pgCjht /!53!boe!54!dbo!brhp!cf!dpot jef af e/!Tqf djCdbraz-!uif!dibabduf ajt yid!bn pvoupguif ijn bhf!boe!uif!qpt jujpo poluif!yin f!byjt!baf!dpot jef af e!up!qaf qbaf!blofx!f wbmbujpo!gvodypo-!tp!uibuuif!af af af odf!gabn f!dbo!cf!ef uf an jof e/ _bluijt!dbtf-!f wfoxiffoluif!gabn f!pqyin vn !po!uif!yinf!byjt!ibt!bo!vodrhbsijn bhf!r vbrjoz-!uif!hf of sbrazelpqyin vn !jn bhf dbo!cf!tfrhdufe/
 - \1389^ Bt left dsicfelbcpwf-lbddpsejohlupluif!fjhi ui!boelojoui!fn cpejn fout-!czltfujohluif!tjohmilsfgfsfodf!gebn fbt!uif!sfgfsfodf!pgdpn qbsjtpo!xjui!uif!gebn ft!gepn!b!qmsbmizz!pgtupsfelgebn ft!cbtfelpo!uif!dibsbdufsjtujd!bn pvouboelijn fbldpssfmbujpo!pguifijn bhf-lop!fsspst!bsfbbdvn vmbufelevsjohluif!wfdupsdbmdvmbujpo/!Fwfoxifolbo!vodmbsgebn ffyjtut-!fydfmmoultzouiftjt!dbo!cf!sfbmj{felxjuipvuboz!qspcmn/
 - \138: ^ B!t upshif!n f ejvn !x jmlof yucf!eft dsjcfe!bt!bopu f slf n cpejn f oulpgu f !qsf t f ouljowf oujpo/
 - \1391^ Fbdi !pgu f !Öxt uluplojou !f n cpejn f out !pgu f !qsf t f oujowf oujpo!dbo!brtnp!cf !bdi jf wf e!cz!i bsex bsf !dpot ujuvujpo-pstcz!b!dpn qvuf st zt uf n !dpot ujuvuf e!pgDQV!boe!n f n psz/
- \1392^ blú floot ýuvýpolpgú flopn qvú statún-lú fln fn psaldpot ýuvú tlú flt upsbhfln fejvn lbddpsejohluplú f qsftfodjowfoýpo/!TqfdjÖdbrozlú flpckfdutlpgú flqsftfodjowfoýpoldbolcflbdi jfwfelczlvtjohljolú fltatún lpslú f bqqbsbuvtlú flt upsbhfln fejvn ljolx i jdi lú flqsphsbn ldpeflpgt pgx bsflgpsfyfdvýohlú flpqfsbýpotleftdsjcfeljolú fn cpejn foutljtlt upsfe-lboelczlsfbejohlboelfyfdvýohlú flqsphsbn ldpeflt upsfeljolú flt upsbhfln fejvn lczlú fltatún

qjudi !jo!t bje!qsf ef uf sn jof e!sf t pmujpot -!boe!pvuqvujoh!ui f !t f dpoe!n pujpo!wf dupsf

6

31

41

56

66

- 6/ B!n f ti pe!bddpsejoh!up!dmjn !5-!x i f sfjo!jo!t bje!ef tf dtjoh!t tf q-!ti f !ovn cf slpggsbn f t !cf ux f f o!ti f !ux p!gsbn f t x i jdi !bsf !pclf dtt !gpslef tf dtjoh!t bje!Öst un ptjpo!wf dtpsk/bo!cf !t x juli f e!jo!bddpsebodf !x jti !b!t j{f !pgt bje!ef tf dtf e Öst un ptjpo!wf dtpsf
- 7/ Bin f ti pelbddpsejohlupldrbjn l3-lx i f sf jolt bjelef tf dyohlt tf qldpn qst f t lt tf qt lpgef tf dyohlt bjeln pypolwf dupslyt joh bolpsi phpobrusbot gpsn ldpf gDtjf oulpcubjof elcz!psi phpobrusbot gpsn johlt bjelux plgsbn f t lpgjn bhf t /
- 8/ B!n f u pelbddpsejoh! wldrbjn !7-lx i f sf jo!t bje!ef uf dujoh!t uf q!dpn qst f t !t uf qt !pg qf spsn joh!uf n qrbuf !n budi joh cf ux f f o!t bje!ux p!gsbn f t !pgjn bhf t !wlspvhi rzlef uf dut bje!n pujpo!wf dwps!boe! Cof rzlef uf dujoh!t bje!n pujpo!wf dwps vt joh!u f !spvhi !ef uf dujpo!sf t vraboe!u f !psu phpobrusbot gpsn !dpf gDdjf oulpgt bje!ux p!gsbn f t /
- 9/ Bh fu pelbddpsejohlupkdrbjn 13-bc i fsf jolt bjelefuf dujohlt uf qktpn qsjt ft lt uf qt lpglefuf dujohlu i fln pujpo Mf dupskof ux f f o
 ui fljn bhf !pglb!sf gf sf odf !gsbn f !bt !pof !pglb!qrmsbrjmz!pggsbn ft !boe!ui fljn bhf !pglf bdi !pglu f !sf n bjojohlgsbn ft -!boe
 t bjelgosn johlt uf q!dpn qsjt ft !t uf qt !pggosn joh!ui fljn bhf !t zou ft j{fe!po!ui fljn bhf!pglt bjelsf gf sf odf!gsbn f!vt joh
 ui fljn bhf!pglui fldpssft qpoejohlgsbn flboe!ui flefuf dufe!n pujpo!wf dupsf
 - :/ Bin fui peloddpsejoh kup klimbjn 19-bx i fsfjolk bjeljo qvujoh ktuf qklpn qsjtft ktuf qt bygkt fmid yoh bpof bybn fbot ktbje ksfgfsfodf gybn fbypn ktif kpmisbrjnz bygejggfsfoubybn ftljo klpo vjov pvt bn pvjpoljn bhftljo b ddpsebo dfbx jui ktif kjn bhf bygfb di bybn f/
 - 21/Bln fü pelbddpsejohlupldmbjn b.-bx i fsfjoltbjelsfgfsfodflogbn fljtltfmldufelospn bibjelopmsbrjoozlopgebn ftljolbddpsebodfx ju lfehflusfohuitlpguifljn bhftljoltbjelopmsbrjoozlopgebn ft/
- 36 22/ Bin f u pe!bddpæjoh!wildrbjn !2-bx i f sf jo!t bje!gosn joh!t uf q!dpn qsjt f t !t uf qt !pgt zou f t j{ joh!bo!jouf sqprbujpo!jn bhf gosn f e!vt joh!pu f sljn bhf t !x ju !sf t qf dulup!b!sf g sf odf !jn bhf !bt !pof !pgt bje!qrmsbrjnz!pgjn bhf t !wp!qsf qbsf !t bje of x !jn bhf /
 - 23/ B!n f u pe!bddpsejoh!up!drbjn !22-!x i f sf jo!t bje!pu f sljn bhf !jt !vt f e!bt !juljt !bt !t bje!jouf sqprbujpo!jn bhf /
 - 24/ B!n f u pe!bddpsejoh!up!dnbjn !22-!x i f sf jo!t bje!jouf sqpmbujpo!jn bhf !jt !gpsn f e!vt joh!t bje!sf gf sf odf !jn bhf !boe!t bje pu f sljn bhf t /
- 25/ Bin f u pelbddpæjohlupldrbjn 124-bx i f sf jolt bjeljouf saprbujpoljn bhf ljt lpcubjof elcztt zoui f t j{ johljogpan bujpolsf hbæjoh t bjelpui f sljn bhf t lupljogpan bujpolsf hbæjohlt bjelsf gf sf odf ljn bhf ljolbddpæbodf lx jui lt bjelsf rbujwf lapt jujpot /
 - 26/ Bin f u pelbddpsejoh lipidnojn 125-ix i f sf jolt bjeljouf sapnaujpoljn bhf ljt lpcubjof elczlt zou i f t j{johloldi bsbduf sjt ujdlwbnwf pgt bjelsf gf sf odf ljn bhf lboeldi bsbduf sjt ujdlwbnwf t lpgt bjelpu f sjn bhf t ljolbddpsebodf lx ju lt bjelsf naujwf lapt jujpot /
- 51 27/ B!n f ui pe!bddpsejoh!up!drbijn !25-b: i f sf jo!t bje!jouf sqprbuijpo!jin bhf !jt !pcubjof e!cz!t zou f t j{joh!bo!psui phpobrhosbot. gpsn !dpf gDdjf out !pcubjof e!gspn !t bje!sf gf sf odf !jin bhf !boe!psui phpobrhosbot gpsn !dpf gDdjf out !pcubjof e!gspn !t bje!pui f s jn bhf t !jo!bddpsebodf !x jui !t bje!sf rbujwf !qpt jujpot /
 - 28/ B!n f u pe!bddpsejoh!up!drbjn !22-!x i f sf jo!t bje!jouf sqprbuypo!jn bhf !jt !pcubjof e!cz!jouf sqprbuyoh!jn bhf !jogpsn buypo jo!t bje!pu f sljn bhf t /
 - 29/ Bin f u pelbddpæjohlupidrbjn 128-ix i f sf jolt bjeljouf saprbujpoljn bhf lit lpcubjof elczljouf saprbujohlu f lin bhf ljogosn bujpo sf hbæjohlt bjelpu f sijn bhf t ljolbddpæbodf ix ju ilt bjelsf rbujwf lapt jujpot /
- 61 2: / B!n f u pe!bddpsejoh!up!drbjn !22-lx i f sf jo!t bje!joqvujoh!t uf q!dpn qsifft!t uf qt !pgtf rfidujoh!pof !jn bhf !bt !t bje!sf g f sf odf !jn bhf !gspn !t bje!qrnsbrjuz!pgjn bhf t !jo!bddpsebodf !x ju !f bdi !jn bhf /
 - 31/ Bln f u pelbddpsejohlupldrbjn !2: -lx i f sfjolt bjelsf gf sf odf ljn bhf ljt lt f rhduf elgepn !t bjelqnmsbrjnz!pgjn bhf t ljolbddpse. bodf !x ju !jn bhf !f ehf !t usf ohu t !jolt bjelqnmsbrjnz!pgjn bhf t /
 - 32/ Bln f ü pelbddpsejohlupldrbin !2: -lx i f sf jolt bjelsf gf sf odf ljn bhf ljt lt f rhduf elgspn lt bjelqmsbrjnzlpgjn bhf t ljolbddpse. bodf !x ju !joqvulpsef slpgt bjelqmsbrjnzlpgjn bhf t /

33/ Boljn bhf !qspdf t t joh!n f u pe-!dpn qsjt joh!t uf qt !pg

6

21

26

31

36

46

51

)b*!joqvujoh!b!qmsbrjoz!pgn vuvbrozlejgf sf oujn bhf t !i bwjoh!qsf ef uf sn jof e!sf t prnujpot <
)c*!gsn joh!bo!jouf sqprtaujpo!jn bhf !gspn !uf f!qmsbrjoz!pgjn bhf t
boe
)d*!gsn joh!b!of x !jn bhf !i bwjoh!b!i jhi !sf t prnujpo!bt !dpn qbsf elx ju !t bje!qsf ef uf sn jof e!sf t prnujpot !cz!t i jgjoh
boe!t zouf t j{joh!uf f!jouf sqprtaujpo!jn bhf !x ju !sf t qf duup!b!sf gf sf odf !jn bhf !bt !pof !pgt bje!qmsbrjoz!pgjn bhf t
x ju !b!sf t prnujpo!rht t !u bo!b!qjyf rhqjudi !jo!t bje!qsf ef uf sn jof e!sf t prnujpo!

- 34/ B!n f u pe!bddpsejoh!up!dnbjn !33-!grsu f sldpn qsjtjoh!b!t uf q!pglef uf dujoh!sf nbujwf !qpt jujpot !bn poh!u f !qnnsbnjnz!pg jn bhf t -!boelx i f sf jo!b!t i jg!bn pvoulpgt bje!jouf sqpnbujpo!jn bhf lx ju !sf t qf dulup!t bje!sf gf sf odf !jn bhf !jt !ef uf sn jof e jo!bddpsebodf !x ju !u f !sf nbujwf !qpt jujpot /
 - 35/ Bin für pelbddpsejohlupldrbijn l34-lx i faf jolt bjelt uf qlpggran johlui f ljouf sqprbujpoljn bhf ldpn qajt fit lt uf qt lpgt zou fit j{johlpsi phpobrhusbot gran ldpf godijf out lpcubjof elgspn lt bjelqrvnsbrjuz lpgjn bhf t luplpcubjolt bjeljouf sqprbujpoljn bhf /
 - 36/ Bln fui pelbddpsejohlupldrbjn l35-lx i fsfjolu fltzou ftjfjohlpgt bjelpsu phpobrhusbot gosn ldpf gÖdjf out ljt lqf sgosn fe x jui lblsbujplgoslblgafr v fodzlbaf blpgf bdi lpsu phpobrhusbot gosn ldpf gÖdjf out
 - 37/ B!n f u pe!bddpsejoh!up!dnijn !36-!x i f sf jo!u f !t zou f t j{joh!pdt bje!psu phpobrhusbot gsm !dpf gDtjf out !jt !qf sgsm f e cz!t f rhdijoh!u f !psu phpobrhusbot gsm !dpf gDtjf out !pcubjof e!gspn !t bje!qrwsbrjuz!pdjn bhf t !jo!bddpsebodf !x ju !u f gf r v f odz!bsf b!pdf bdi !psu phpobrhusbot gsm !dpf gDtjf out
 - 38/ Boljn bhf laspdf t t johln f u pe-lapn ast johlt uf at lpg

) b*!fyusb dyoh!b!qnnsb njoz!pgsbn ft!gspn!n pujpo!jn b hft!i bwjoh!qsfefufsn jofe!sftpnnujpot <
) c*!db ndv nbujoh!psuiphpob nbusbot gosn!dpf godijfout!pgfbdi!pgjn b hft!jo!uif!qnnsb njoz!pggsbn ft

| belsft dyoh!n pujpo!wfdupst!bn poh!tbje!qnnsb njoz!pggsbn ft!xjui!b!sftpnnujpo!nfntt!uibo!b!qjyfnnujudi!jo!tbjeqsfefufsn jofe!sftpnnujpot!cz!vtjoh!uif!psuiphpob nbusbot gosn!dpfgodijfout/

- 41 39/ B!n f u pelbddpsejoh! wldrinin !38-!x i f sf jo!t bjelef uf dyoh!t uf q!dpn qstft!t uf qt !pgqf sgpsn joh!uf n qrbuf !n budi joh cf ux f f o!t bje!ux p!gsbn f t !pgjn bhft !wp!spvhi rz!ef uf dut bje!n pujpo!wf dups!boe!Obf rz!ef uf dyoh!t bje!n pujpo!wf dups vt joh!uf !spvhi !ef uf dypo!sft vrdboe!uf !psi phpobrhusbot gpsn !dpf godjf out !pgt bje!ux p!gsbn f t /
 - 3: / Boljn bhf !qspdf t t joh!n f u pe-!dpn qsjt joh!t uf qt !pg

) b*ljoqvujoh!b!qmsbrjnoz!pgn vuvbmoz!ejggf sfouljn bhft!i bwjoh!qsfef uf sn jofe!sft pmyupot <
) c*!dbrodvmoujoh!psu phpobmusbot gosn !dpf gÖdjf out!pgf bdi !pgu f !qmsbrjnoz!pgjn bhft dboe
) d*!tijgjoh!boe!t zou ftj{joh!t bje!qmsbrjnoz!pgjn bhft!x ju !b!sft pmyupo!mftt!u bo!b!qjyf mlqjudi !jo!t bje!qsfef ufs n jofe!sft pmyupot-!cz!vtjoh!u f!psu phpobmusbot gosn !dpf gÖdjf out/

- 41/ B!n f u pe!bddpsejoh!up!drbjn !3: -!g/su f sldpn qsjt joh!b!t uf q!pgef uf dujoh!sf rbujwf !qpt jujpot !bn poh!t bje!qrmsbrjuz!pg jn bhf t !boelx i f sf jo!t bje!t zou f t j{joh!t uf q!dpn qsjt f t !t uf qt !pgt zou f t j{joh!t bje!qrmsbrjuz!pgjn bhf t !jo!bddpsebodf x ju !t bje!sf rbujwf !qpt jujpot /
- 42/ B!n f u pelbddpsejoh!upldrbjn !41-!x i f sf joljo!t bje!t zou f t j{joh!t uf q-!u f !t zou f t j{joh!pg u f !psu phpobrhusbot gosn dpf godjf out !jo!t bje!qrwsbrjuz!pgjn bhf t !jt !qf sgosn f e!x ju !b!sbujp!goslb!gsf r vf odz!bsf b!pgf bdi !pg u f !psu phpobrusbot gosn !dpf godjf out /
- 43/ B!n f u pe!bddpsejoh!up!drbjn !42-!x i f sf jo!u f !t zou f t j{joh!pdt bje!psu phpobrhusbot gsn !dpf gDdjf out !jt !qf sgpsn f e cz!t f rhdujoh!u f !psu phpobrhusbot gsn !dpf gDdjf out !pcubjof e!gspn !t bje!qmsbrjuz!pdjn bhf t !jo!bddpsebodf !x ju !u f gsf r v f odz!bsf b!pdf bdi !psu phpobrhusbot gsn !dpf gDdjf out
 - 44/ Boljn bhf lqspdf t t johlbqqbsburt -ldpn qsjt joh;

b)*ijoqvun f bot !gsljoqvujoh!b!qmsbrjnz!pgn vuvbnazlejgf si oljn bhf t !i bwjoh!qsi ef uf sn jof e!si t pnnijpot
)c*lef uf dijoh!n f bot !gslef uf dijoh!si rbujwi !qpt jijpot !bn poh!ui f !qnmsbrjnz!pgjn bhf t !x jui !b!si t pnnijpo!ntt t !ui bo b!qjyf ntqjudi !jo!t bje!qsi ef uf sn jof e!si t pnnijpot
boe
)d*!gsn joh!n f bot !gslgsn joh!b!of x !jn bhf !i bwjoh!b!i jhi !si t pnnijpo!bt !dpn qbsi e!x jui !t bje!qsi ef uf sn jof e

sf tpmujpot lczlvtjohltbjelqmashnjozlpgjn bhf tljolbddpæbodflxju ljogosn bujpoljoejdbujohlu flsf mbujwflqptjujpot ospon lu flef ufduohln fbot/

- 45/ Bolbqqbsbwt !bddpsejoh! wldrbin !44-!x i f sf jo!t bje!qrvsbrjrz!pgjn bhf t !sf rbuf !wl.x p!ejgf sf oulgebn f t !jo!n vuvbrandpoyovpvt !n pypo!jn bhf t -!boe!t bje!ef uf dyoh!n f bot !ef uf dut !ui f !jogpsn bypo!joejdbyjoh!t bje!sf rbujwf !qpt jypot !bt b!n pypo!wf dws
- 46/ Bolbqqbsbwt !bddpsejoh!upldrbjn !45-!x i f sf jo!t bje!ef tf dujoh!n f bot !ef tf dut !t bje!n pujpo!wf dups!vt joh!psu phpobmusbot gpsn !dpf qddif out !pcubjof e!cz!psu phpobmzlubot gpsn joh!t bje!ux p!gsbn f t !pgjn bhf t/
- 47/ Bolbqqbsbwt lbddpsejohlupldrbjn 144-brif sfjolt bjelgosn johln f bot lt zou f tj{ft lboljouf sqprbujpoljn bhf lgosn f elvt joh pu f sljn bhft lx ju lsf t qf duluplb!sf gf sf odf ljn bhf lbt lpof lpgt bjelqrmsbrjoz!pgjn bhft luplqsf qbsf lt bjelof x ljn bhf/
- 48/ Bo!bqqbsburt!bddpsejoh!\p!drbjn !47-!x i f sf jo!t bje!\psn joh!n f bot !t zou f t j\{f t !jo\psn b\pio!sf hb\text{spio!t bje!pu f s jn bhf t !x ju !sf t qf du\p!jo\psn b\pio!sf hb\text{sejoh!t bje!pu f s jn bhf t !x ju !sf t qf du\p!jo\psn b\pio!sf hb\text{sejoh!t bje!sf g sf odf !jn bhf !jo!bddp\text{sebodf !x ju !t bje!sf rb\pi\wf !qpt j\piot !\pi pc\pioj!t bje!jouf sqpr\text{bqpr\text{bq}po!jn bhf /}
- 49/ Bolbqqbsbwt !bddpsejoh!p!drbjn !48-lx i f sf jolt bje!gran joh!n f bot !t zou f t j{f t !bo!psi phpobrhusbot gran !dpf gDdjf ou pcubjof e!gran !t bje!sf gf sf odf !jn bhf !boe!psi phpobrhusbot gran !dpf gDdjf out !pcubjof e!gran !t bje!pu f sljn bhf t !jo bddpsebodf !x ju !t bje!sf rbujwf !qpt jupot !up!pcubjo!t bje!jou sqprbujpo!jn bhf /
- 4: / Boljn bhf !qspdf t t joh!bqqbsbwt -!dpn qsjt joh;

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-)b*ljoqvujoh!n f bot !gɔsljoqvujoh!b!qnnsbrjuz!pgn vuvbnuzlejgf sf ouljn bhf t !i bwjoh!qsf ef uf sn jof e!sf t prnujpot <)c*!Œxt dgɔsn joh!n f bot !gɔslgɔsn joh!bo!jouf sqprbujpo!jn bhf !gspn !ui f !qnnsbrjuz!pgjn bhf t ⊀boe)d*!t f dpoe!gɔsn joh!n f bot !gɔslgɔsn joh!b!of x !jn bhf !i bwjoh!b!i jhi !sf t prnujpo!bt !dpn qbsf e!x jui !t bje!qsf ef uf sn jof e!sf t prnujpot-!cz!t i jgjoh!boe!t zoui f t j{joh!ui f !jouf sqprbujpo!jn bhf !x jui !sf t qf ddup!b!sf gf sf odf !jn bhf !bt pof !pgt bje!qnnsbrjuz!pgjn bhf t !x jui !b!sf t prnujpo!rft t !ui bo!b!qjyf rhqjudi !jo!t bje!qsf ef uf sn jof e!sf t prnujpot /
- 51/ Bolbqqbsbuvt !bddpsejoh!up!dmbjn !4: -lgvsuifsldpn qsjtjoh!ef ufdujoh!n fbot!goslef ufdujoh!sfmbujwf!qptjujpot!bn poh!uifqmsbnjoo:lpdjn bhft-!boe!x ifsfjo!tbje!tfdpoe!gosn joh!n fbot!efufsn joft!bltijg!bn pvoulpgtbje!joufsqpmbujpo!jn bhfx jui!sftqfddup!tbje!sfgfsfodf!jn bhf!jo!bddpsebodf!x jui!uif!sfmbujwf!qptjujpot/
 - 52/ Bologqbsbuvt boldpsejoh lupklimbjn !51-bx i f.sf.jo ht bje!Öut ulgosn joh hn f bo t ht zou i ft j{ft hpsui phpob musbo t gosn ldpf gÖdjf out pcubjof elgenn !t bje!qm/sbm/wz!pgjn bhft!up!pcubjo!t bje!jouf sqp/mujpo!jn bhf/
 - 53/ Boljn bhf !qspdf t t joh!ef wjdf -!dpn qsjt joh;
 -) b*lf yuzb dyoh In fbotlop stryuzb dyoh Ib kqm sbrjoz Ipgobon ftlosp n In pypoljn b hftli bwjoh kqsfefufsn jofelsft pmujpot<) c*ldb notwnbujoh In fbotlop stdb notwnbujoh Ipsuiph po b mbabotop sn ldpfoldjfoutlp gfbdilp gjn b hftljoluiflam sbrjoz Ipg gbon ft⊰boe
 -)d*lef uf dujohln f bot lyoslef uf dujohln pujpolwif dupat lbn pohlt bjelqmashrjuz lpggson f t lx jui lblaf t prnujpolvifut t lui bolb qjyf rhqjudi ljolt bjelqaf ef uf an jof elaf t prnujpot -lcz!vt johlui f lpau phpobruasbot goan ldpf gDdjf out/
- 56 54/ Bolin bhf laspdf t t johlef widf -ldpn asit joh;
 -)b*ljoqvujoh!n f bot !gosljoqvujoh!b!qnnsbnjoz!pgn vuvbnozlejggf sfouljn bhft!i bwjoh!qsfefufsn jofe!sftpmujpot <
)c*!dbrokvnbujoh!n f bot !gosldbrokvnbujoh!psu phpobrhosotgosn !dpfgÖdjfout!pgfbdi !pguff!qnnsbnjoz!pgjn bhft dboe
)d*!t zou ftj{joh!n f bot !goslti jgjoh!boe!t zou ftj{joh!t bje!qnnsbnjoz!pgjn bhft!x ju !b!sftpmujpo!rhtt!u bo!b!qjyfm
 qjudi !jo!t bje!qsfefufsn jofe!sftpmujpot-!cz!vtjoh!u f!psu phpobrhosbotgosn !dpfgÖdjfout/
 - 55/ Blsf dpsejohln f ejvn lsf beborfnlczlbldpn qvtf slx i jdi lt tpsf t lblqsphsbn lgpslqf sgpsn johlblqspdf t t johlqspdf t t ldpn . qst johlt tf qt lpg
 -) b*ljoqvujoh!b!qnasbnjoz!pgn vuvbnozlejggfsfouljn bhft!i bwjoh!qsfefufsn jofe!sftpmujpot<) c*lefufdujoh!sfnbujwf!qptjujpot!pguif!qnasbnjoz!pgjn bhft!xjui!b!sftpmujpo!nfntt!uibo!b!qjyfnbujudi!jo!tbje!qsfef. ufsn jofe!sftpmujpot⊰boe
 -)d*losn johlblof x lin bhf li bwjohlbli jhi lsf t praypolbt ldpn qbsf elx ju lt bjelqsf ef uf sn jof elsf t praypot lvt johlt bje

qmsbrjuz!pgjn bhf t!jo!bddpsebodf!xjui!jogosn bujpo!joejdbujoh!uif!sfrbujwf!qptjujpot!pcubjofe!jo!uif!efufdujoh

56/ Blsf dpæjohln f ejvn lsf bebcmlczlbldpn qvtf slx i jdi lt tpsf t lblqsphsbn lgpslqf sgpsn johlblqspdf t t johlqspdf t t ldpn . qsjt johlt tf qt lpg

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) b*ljoqvujoh!b!qmsbnjnz!pgn vuvbmozlejgf sfoujn bhf t !i bwjoh!qsfef uf sn jofe!sft pmujpot <
) c*lgpsn joh!bo!jouf sqpmbujpo!jn bhf !gpn !ui f !qmsbnjnz!pgjn bhf t ≺boe
) d*lgpsn joh!blof x ijn bhf ii bwjoh!b!i jhi !sft pmujpo!bt !dpn qbsfebx jui !t bje!qsfef uf sn jofe!sft pmujpot-!cz!t i jgjoh
boe!t zou f t j{joh!ui f !jouf sqpmbujpo!jn bhf !x jui !sft qfddup!b!sfgf sfodf !jn bhf!bt!pof!pgt bje!qmsbnjnz!pgjn bhf t
x jui !b!sft pmujpo!ntt t !ui bo!b!qjyfntqjudi !jo!t bje!qsfef uf sn jofe!sft pmujpot/

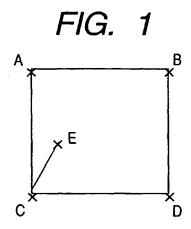
57/ Blsf dpsejohln f ejvn lsf beborfnlczlbldpn qvtf slx i jdi lt upsf t lblqsphsbn lgpslqf sgpsn johlblqspdf t t johlqspdf t t ldpn . qst johlt tf qt lpg

)b*!fyuobdyoh!b!qmusbrjooz!pgosbn ft!gopn !n pujpolj!n bhft!i bwyoh!qsfefufsn jofe!sftpmujpot<
)c*!dbrodvrbuyoh!psuiphpobrhosbotgosn !dpfgÖdjfout!pgfbdi!pgjn bhft!jo!uif!qmusbrjooz!pgosbn ft⊲boe
)d*!efufdyoh!n pujpo!wfdupst!bn poh!tbje!qmusbrjooz!pgosbn ft!xjui!b!sftpmujpo!mftt!uibo!b!qjyfmlqjudi!jo!tbje
qsfefufsn jofe!sftpmujpot-!cz!vtjoh!uif!psuiphpobrhosbotgosn!dpfgÖdjfout/

58/ Blsf dpsejohln f ejvn lsf beborfnlczlbldpn qvuf slx i jdi lt upsf t lblqsphsbn lgpslqf sgpsn johlblqspdf t t johlqspdf t t ldpn . qsjt johlt uf qt lpg

) b*ljoqvujoh!b!qmàsbnjoz!pgn vuvbnozlejgf sfoujn bhft!i bwjoh!qsfef uf sn jofe!sft pmujpot <
) c*!dbrotvnoujoh!psu phpobuhsbot gpsn !dpf godjf out !pgf bdi !pgu f !qmsbnjoz!pgjn bhft dboe
) d*!ti jgjoh!boe!t zou ftj{joh!t bje!qmsbnjoz!pgjn bhft!x ju !b!sft pmujpo!nfntt!u bo!b!qjyf ntqjudi !jo!t bje!qsfef uf s n jofe!sft pmujpot-!cz!vtjoh!u f!psu phpobuhsbot gpsn !dpf godjf out/

59/ Jh bhf !qspdf t t joh!bqqbsbwt !gslgpsn joh!b!@bthjn bhf !x ju !b!sf t pmypo!i jhi f slu bo!bo!joqvuljn bhf -!u f !bqqbsbwt dpn qst joh!n f bot !gslef uf dijoh!n pipo!wf dipst !cf ux f f o!gsbn f t !pgb!n pwjoh!jn bhf -!boe!jouf sqprbujpo!n f bot !vij. jh joh!ejwjef e!n pujpo!wf dipst !gsljouf sqprbujoh!qjyf m!joup!pof !pgt bje!gsbn f t /

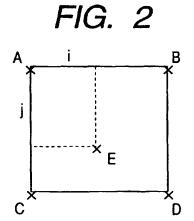


J=MIN(|A-E|, |B-E|, |C-E|, |D-E|)=|X-E|

J IS MINIMUM DISTANCE FROM INTERPOLATION POINT TO OBSERVATION POINT.

X REPRESENTS OBSERVATION POINT WHICH RESULTS IN MINIMUM DISTANCE.

INTERPOLATION POINT E=X



INTERPOLATION POINT $E=(1-i)(1-j)A+i\cdot(i-j)B+j\cdot(1-i)C+ijD$

FIG. 3

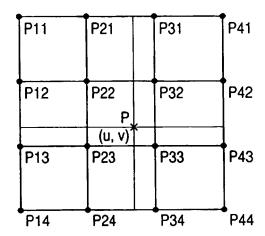
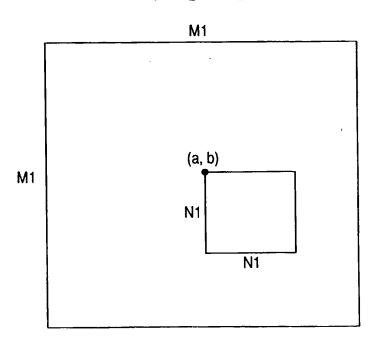
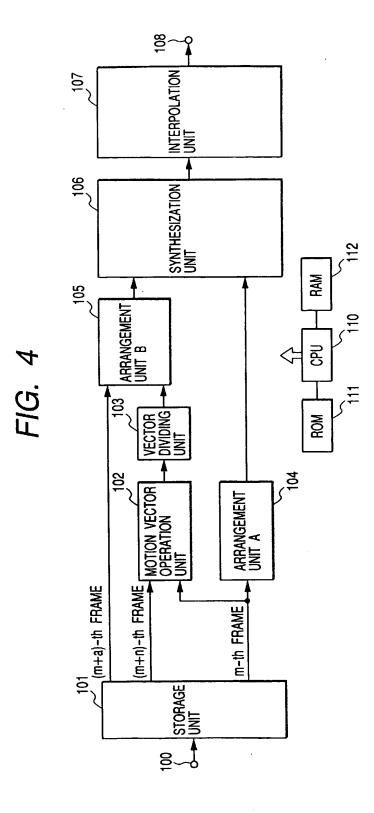
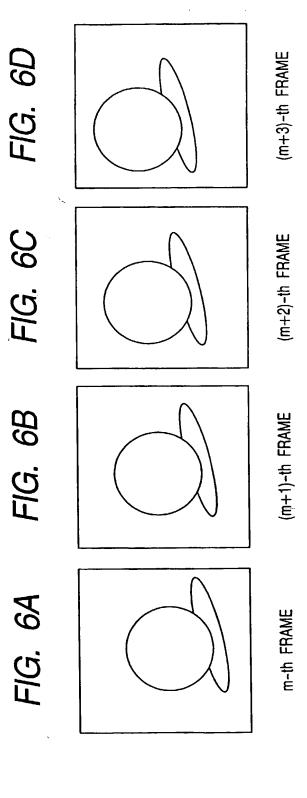


FIG. 5







j

FIG. 7A

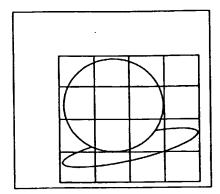


FIG. 7B

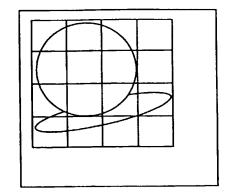


FIG. 7C

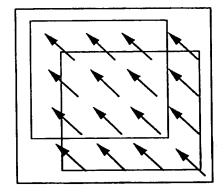
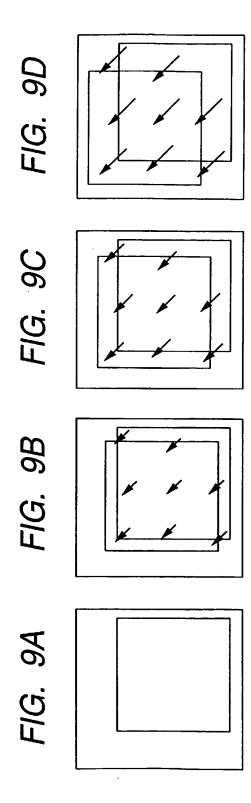


FIG. 8A FIG. 8B FIG. 8C









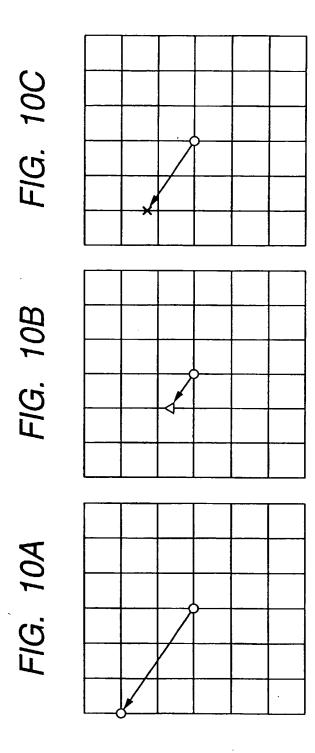
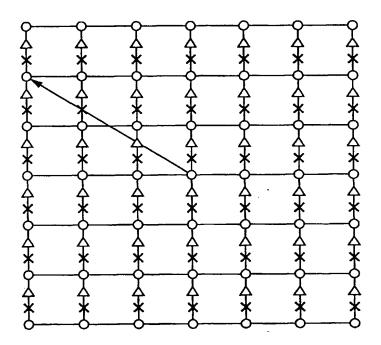
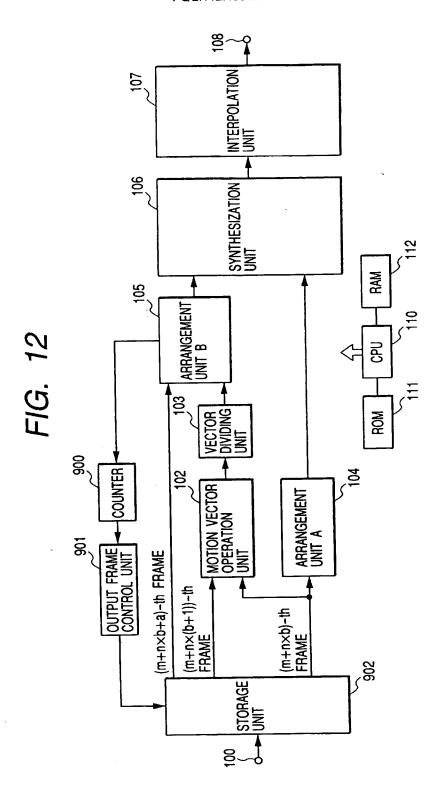


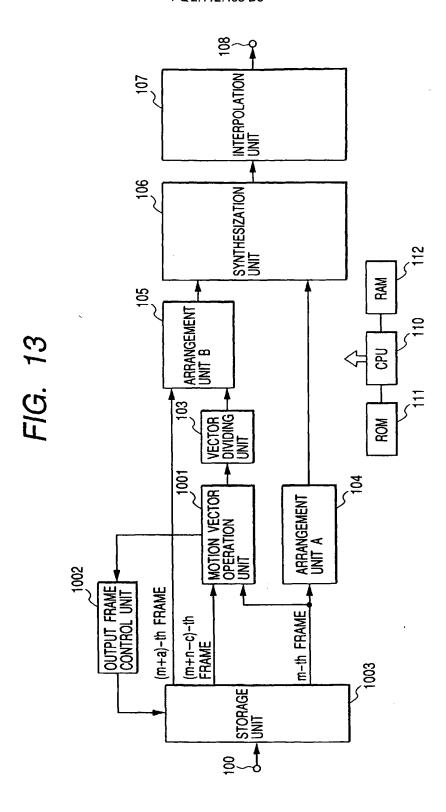
FIG. 11

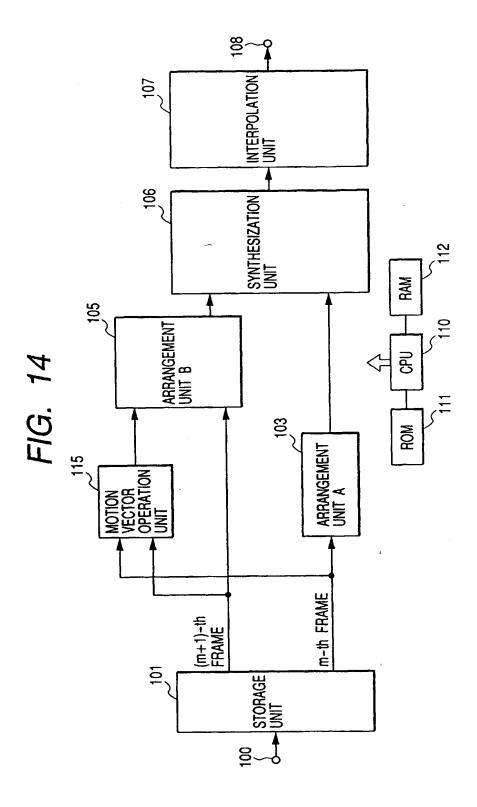


o: m-th FRAME

△: (m+1)-th FRAME ×: (m+2)-th FRAME







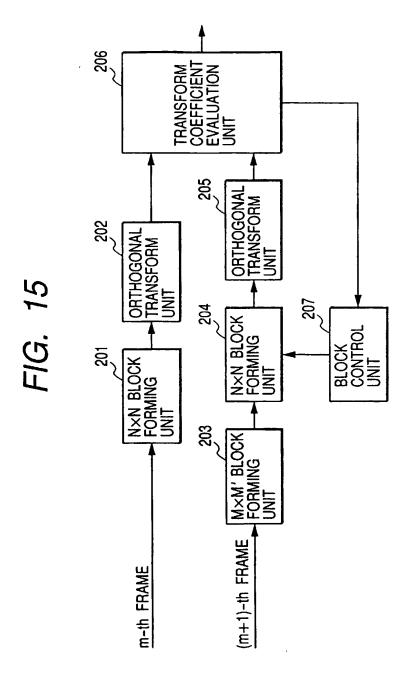


FIG. 16

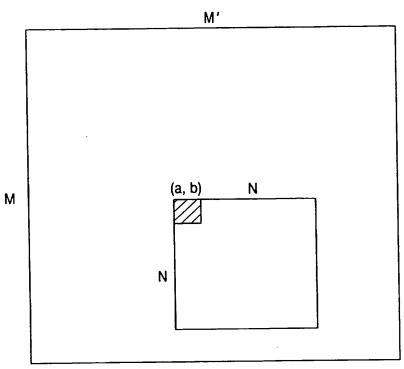
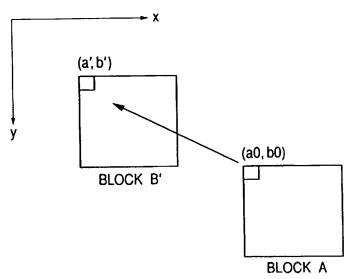
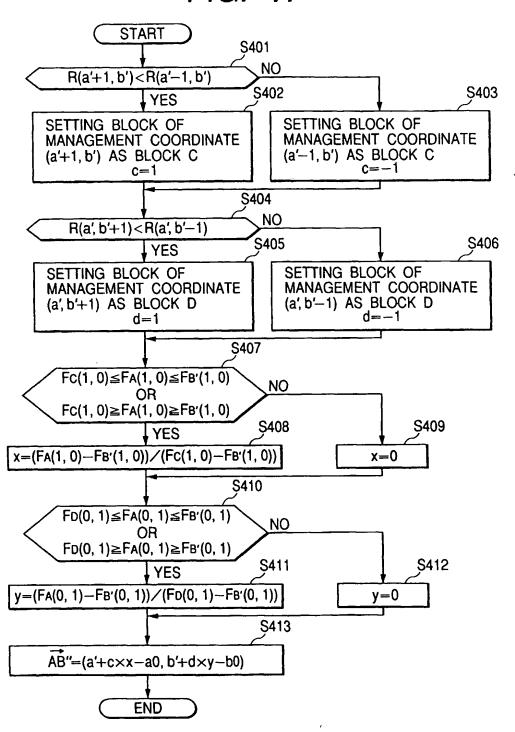
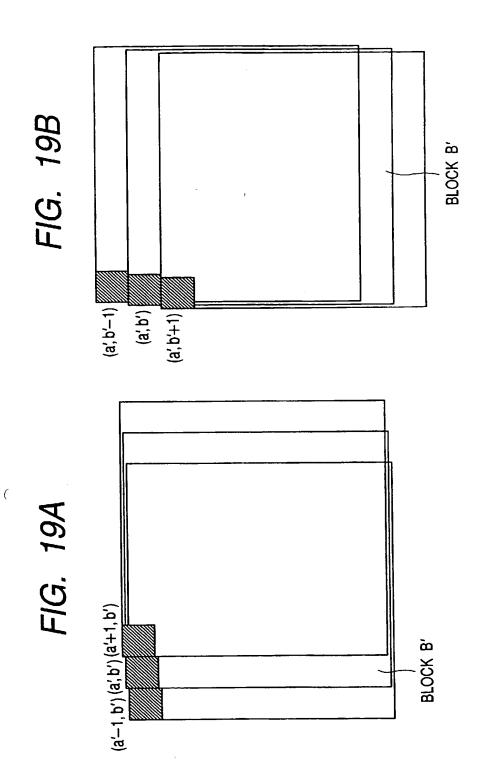


FIG. 18





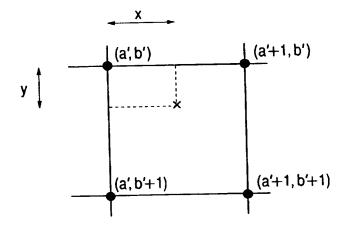


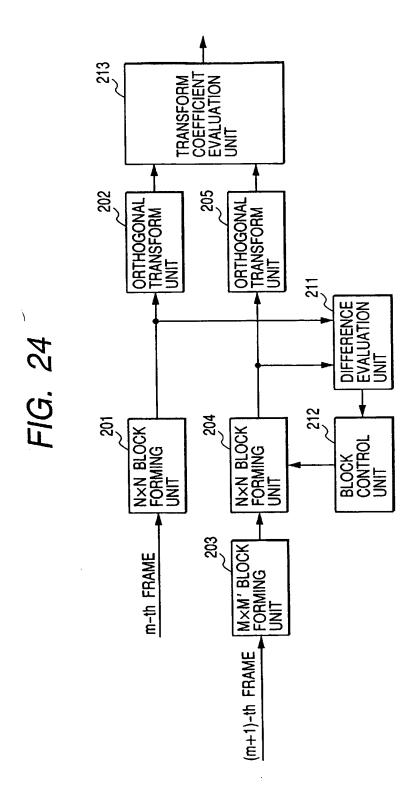
(BLOCK	Α							
	1N 63 62 81 102 125 134 137 144	56 73 91 103 121 140 142 145	60 73 99 102 116 140 147 145	54 75 105 103 111 120 137 140	52 83 112 105 112 110 112 114	50 90 117 109 110 106 107 106	46 96 121 110 106 105 105	47 99 120 111 103 101 97 88	7 01
	DCT 824.50 -157.84 -66.66 -45.08 -34.75 -9.14 4.34 7.66	36.37 -80.37 32.40 35.71 22.78 8.40 7.21 -0.48	-6.21 7.36 -7.42 8.77 2.11 -2.99 -3.24 -6.23	-10.28 9.76 -6.94 0.01 9.37 -4.30 -0.46 2.47	-9.75 4.70 0.17 -0.79 7.00 0.91 -0.88 2.52	3.45 -8.01 6.01 -1.72 2.06 3.82 0.00 2.11	0.68 1.05 0.76 4.12 1.83 2.45 1.42 0.42	-0.24 2.59 -1.86 3.75 -0.83 -0.25 2.25 0.04	~~~ 702

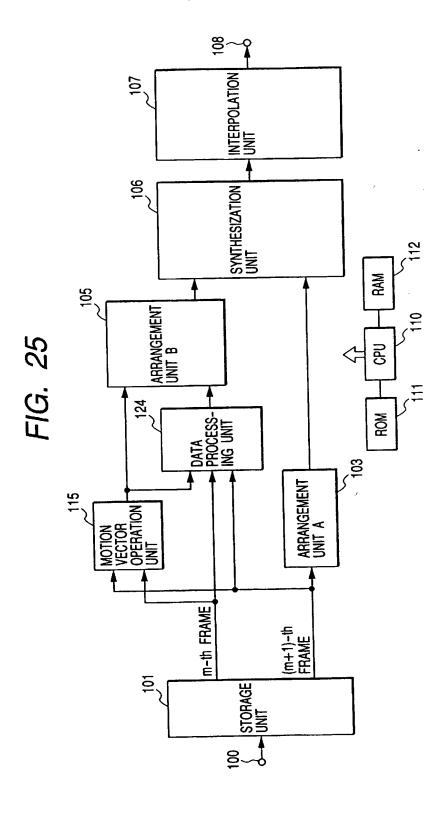
ĺ	BLOCK	В'							
	IN 65 57 80 102 127 132 136 144	54 73 87 103 124 140 140	59 72 98 102 116 142 148 146	56 75 105 103 111 124 140 141	52 82 110 105 112 112 116 114	50 87 115 109 110 106 107 106	46 95 121 110 107 105 105	45 99 122 111 103 101 97 86	~~711
	DCT 824.50 -162.46 -67.59 -42.10 -32.75 -8.12 4.72 8.08	35.50 -80.86 32.17 37.82 25.75 7.79 6.92 -0.45	-9.34 9.85 -9.69 6.31 4.94 -4.68 -2.74 -4.05	-12.17 9.29 -6.17 0.84 13.23 -2.64 -0.36 3.94	-8.25 5.72 0.37 0.07 5.00 3.71 -0.42 3.89	5.78 -8.08 8.03 -2.33 3.22 5.04 2.69 3.05	-1.00 1.59 0.26 3.76 1.47 4.64 2.69 1.09	0.11 1.36 -1.26 2.95 -1.08 0.45 1.94 0.48	<i>→</i> 712

BLOCK C	;							
54 73 87 103 124 140 140 145	59 72 98 102 116 142 148 146	56 75 105 103 111 124 140 141	52 82 110 105 112 112 116 114	50 87 115 109 110 106 107	46 95 121 110 107 105 105	45 99 122 111 103 101 97 86	53 99 116 112 103 99 96 88	<i>~</i> 721
DCT 814.87 -134.83 -76.47 -53.76 -43.62 -10.64 1.23 5.79	41.46 -84.34 32.76 28.31 15.13 7.16 8.44 1.30	6.37 -9.12 2.83 12.19 0.25 -1.27 -2.35 -7.72	-1.61 1.20 -8.35 -0.17 -0.37 -7.14 -0.80 -2.39	-8.62 8.46 -5.58 4.16 7.37 -4.25 -2.69 -1.03	-6.73 5.17 -5.23 -1.87 -1.11 -3.27 -2.52 0.45	2.64 -4.66 4.65 -3.50 3.55 -1.08 -1.58 0.45	-1.23 -0.43 0.58 -1.91 1.19 1.03 -0.93 0.29	~~~ 722

FIG. 23







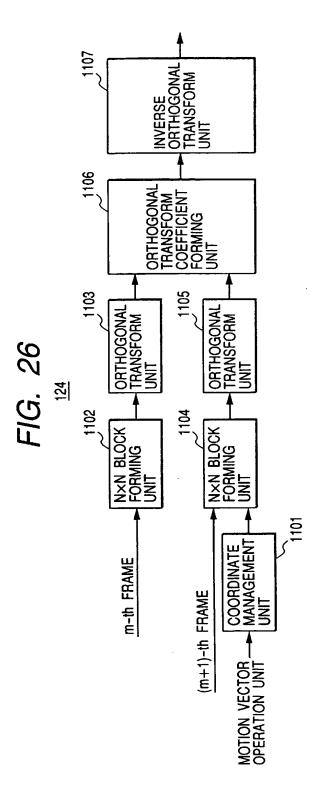
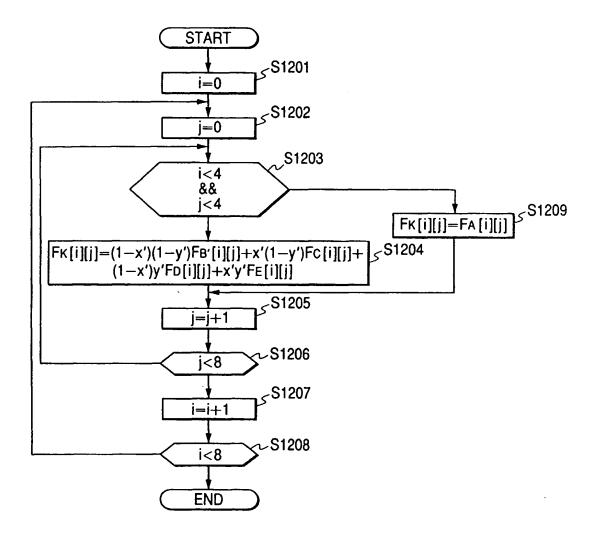
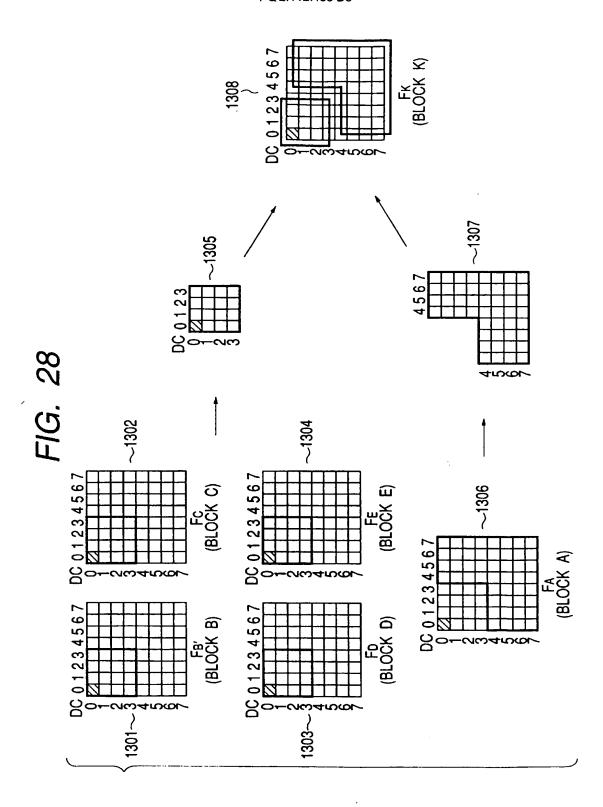


FIG. 27





	BLOCK	Α							
<	IN 188 191 192 189 190 206 199 198	192 190 197 193 195 203 183 171	191 192 205 197 190 146 118 40	192 197 204 187 101 54 51	192 196 188 102 13 45 68 123	198 189 88 0 51 108 145 199	197 114 5 48 117 170 204 196	164 69 40 104 164 202 200 187	~~~ 731
	DCT 1178.50 92.83 112.98 55.63 -11.25 9.15 -1.61 -4.93	174.46 131.72 -170.64 -81.43 -30.26 10.76 5.93 7.42	147.27 -256.40 -1.32 113.39 40.44 -4.63 -2.01 -2.74	-12.12 -41.94 167.87 -45.84 -27.04 -43.49 14.76 -9.43	-29.50 56.76 -44.20 -60.88 9.25 30.41 14.79 -10.99	-21.41 19.60 -24.42 41.36 9.59 10.50 -31.30 1.66	0.15 5.99 -5.76 5.36 -15.40 -18.86 2.57 15.49	2.15 -4.24 -2.32 -2.86 2.65 10.41 4.72 -3.37	~~~ 732

	BLOCK	B'							
7	IN 188 190 191 191 186 193 203 204	186 187 198 193 200 204 190 176	189 186 201 199 198 151 120 31	192 196 199 188 99 47 37	190 205 192 85 0 35 48 103	199 198 80 0 36 106 152 204	206 125 0 26 109 167 206 204	155 62 36 85 161 209 193 188	<u>~~ 741</u>
	DCT 1159.75 95.65 127.18 55.92 -17.00 0.37 -2.62 -4.41	184.32 128.49 -187.82 -88.27 -18.24 22.37 -1.38 10.93	155.88 -276.11 5.86 112.67 40.78 -3.90 -1.25 4.07	-11.60 -31.39 185.38 -57.29 -31.54 -38.99 5.44 -13.99	-47.00 68.09 -49.36 -66.87 11.75 24.69 22.61 -9.83	-15.20 20.30 13.25 40.80 19.71 11.59 35.64 0.43	2.00 -0.33 -13.25 7.49 -13.91 -9.66 -0.86 9.39	-5.70 8.22 -3.28 3.80 -5.83 6.42 7.18 4.71	~~~ 742

				IG.	S I				
(BLOCK	С							
	IN 186 187 198 193 200 204 190 176	189 186 201 199 198 151 120 31	192 196 199 188 99 47 37	190 205 192 85 0 35 48 103	199 198 80 0 36 106 152 204	206 125 0 26 109 167 206 204	155 62 36 85 161 209 193 188	125 26 26 139 207 208 189 190	751
	DCT 1105.25 44.91 117.77 92.27 10.50 4.62 -1.16 -5.17	88.47 277.30 -124.26 -122.98 -64.81 11.15 -3.39 10.38	157.01 -173.52 -186.44 90.11 63.27 29.11 0.64 13.33	82.13 -147.21 141.08 69.97 -21.57 -36.68 -10.89 2.06	14.00 -37.66 69.55 -62.01 -13.25 -23.73 22.88 -7.98	-10.74 16.85 5.52 -44.14 -2.99 10.80 28.72 -9.66	-4.42 -0.88 7.14 4.46 26.02 8.41 -19.56 -9.53	4.15 -4.08 1.86 -3.70 -1.41 -7.89 -4.13 -2.07	~~~ 752
	_		· · · · · · · · · · · · · · · · · · ·	FIG.	32				
1	BLOCK								
		D							
	IN 190 191 191 186 193 203 204 201	187 198 193 200 204 190 176 147	186 201 199 198 151 120 31 6	196 199 188 99 47 37 0	205 192 85 0 35 48 103 170	198 80 0 36 106 152 204 203	125 0 26 109 167 206 204 192	62 36 85 161 209 193 188 194	761

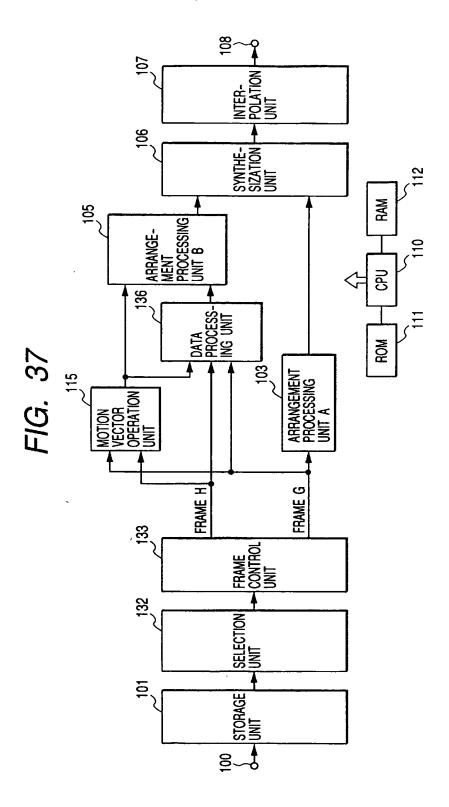
BLOCK	E							
187 198 193 200 204 190 176 147	186 201 199 198 151 120 31 6	196 199 188 99 47 37 0	205 192 85 0 35 48 103 170	198 80 0 36 106 152 204 203	125 0 26 109 167 206 204 192	62 36 85 161 209 193 188 194	26 26 139 207 208 189 190	771
DCT 1064.87 -38.30 25.79 64.99 45.38 10.13 14.89 6.33	21.17 363.34 35.66 -34.36 -64.19 -40.76 -7.03 -16.23	166.91 -46.29 -258.59 -58.78 -1.94 21.58 5.65 -5.69	104.78 -191.47 17.45 112.50 39.81 30.50 -12.65 -0.32	56.88 -85.73 105.41 -2.63 -6.12 -10.73 -26.75 12.47	8.46 -11.08 54.02 -35.73 -13.21 -31.98 -8.72 13.50	-8.93 -7.63 -3.35 -7.98 -5.01 23.54 19.84 5.81	2.86 4.04 -1.00 7.79 -1.45 9.04 -3.30 2.14	~~ 772

	BLOCK	K							
<	DCT 1134.81 62.44 107.96 67.11 -11.25 9.15 -1.61 -4.93	150.17 194.24 -139.26 -88.91 -30.26 10.76 5.93 7.42	165.94 -238.36 -74.05 82.38 40.44 -4.63 -2.01 -2.74	21.62 -84.09 168.01 -1.68 -27.04 -43.49 14.76 -9.43	-29.50 56.76 -44.20 -60.88 9.25 30.41 14.79 -10.99	-21.41 19.60 -24.42 41.36 9.59 10.50 -31.30 1.66	0.15 5.99 -5.76 5.36 -15.40 -18.86 2.57 15.49	2.15 -4.24 -2.32 -2.86 2.65 10.41 4.72 -3.37	~~~ 781
	OUT 184 190 195 196 198 207 190 180	189 191 199 190 182 184 163 154	192 192 199 179 159 114 96 29	197 190 182 157 74 38 46 2	196 179 152 72 8 61 88 137	190 166 58 0 65 140 172 214	168 93 0 57 136 189 215 199	119 52 54 130 179 201 191 178	~~~ 782

FIG. 35 x'=1/4 (a',b') (a'+1,b') (a',b'+1) (a'+1,b'+1)

FIG. 36 START S2101 i=0 S2102 j=0 Fx'[i][j]=(1-x')(1-y')FB'[i][j]+x'(1-y')Fc[i][j]+ (1-x')y'Fb[i][j]+x'y'Fe[i][j] 1∕S2104 $FK[i][j] = \alpha[i][j] \times FK'[i][j] + \beta[i][j] \times FA[i][j]$ S2105 j=j+1 ~S2106 j<8 _SS2107 i=i+1~S2108 i<8

END



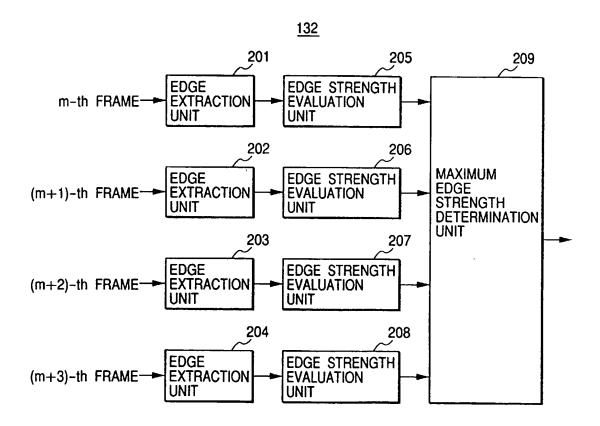
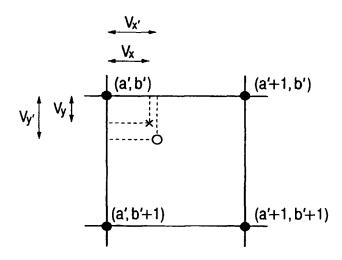
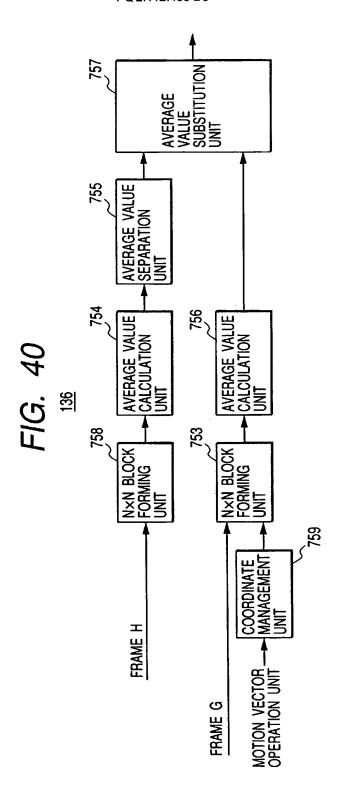


FIG. 39

1	1	1
1	-8	1
1	1	1

FIG. 41





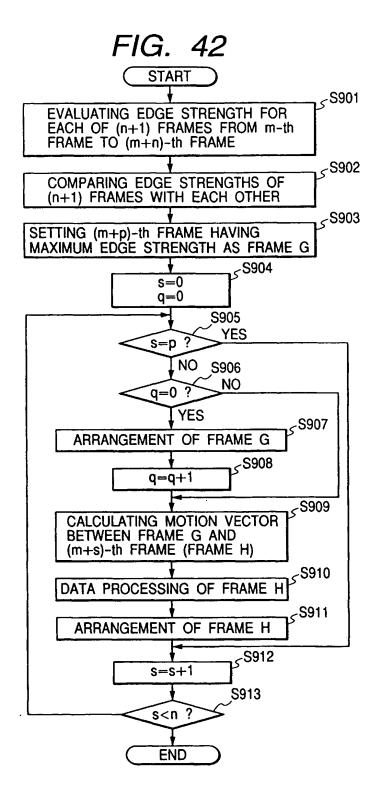


FIG. 43

